



**THE UNIVERSITY OF QUEENSLAND**  
AUSTRALIA

This exam paper must not be removed from the venue

School of Information Technology and Electrical Engineering  
Mid-Term Quiz

**METR4202: ROBOTICS & AUTOMATION**

**S e p t e m b e r 2 0 , 2 0 1 7**

**First Name:** \_\_\_\_\_ **Last Name:** \_\_\_\_\_

**Student Number:** \_\_\_\_\_

Examination Duration: 60 minutes

Reading Time: 10 minutes

**Exam Conditions:**

This is an Open Book Examination

**Electronic Materials Permitted In The Exam Venue:**

- No Internet Connected Devices (laptops, phones, etc.)
- Calculators - Any calculator permitted - unrestricted

**Instructions To Students:**

- Please be sure to place your name and number on **ALL** pages
- Please answer **ALL** questions.
- ⇔ **ALL** Answers **MUST Be Justified** ⇔  
(answers alone are not sufficient)

Thank you! :-)

Q	Mark
1	
2	
3	
4	
5	
6	

Total \_\_\_\_\_

This quiz consists of Multiple Choice, Short Answer, and Worked Problems. **Please Answer All Questions** below on the quiz paper. Answers must be neat and clear. All answers (except for multiple choice) **must provide a brief justification**. You may use the back of each sheet as scratch paper if needed. The total quiz is worth 100 points.

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### Part I: Robot Arm Kinematics (& Frames in Space)

#### 1. A One Dimensional Robot for Question One

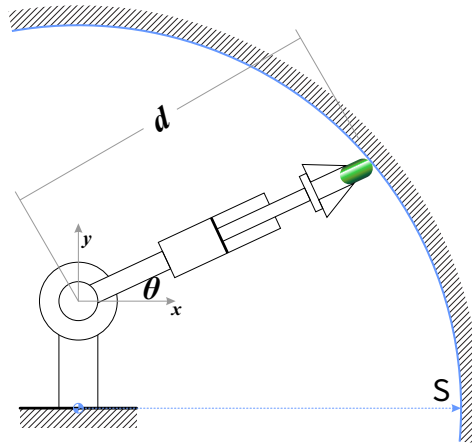
[10 Points]

To get started, imagine a one-dimensional rotary (1R) robot.

- (a) If this robot arm rotates about the **z-axis**, what would its **rotation matrix** (i.e.  $R_O^T$ ) from its Origin {O} to the Tip {T} be for a given rotation value  $\theta^*$ ?
  
- (b) Instead, if this robot arm rotates about the line  $\mathbf{y} = \mathbf{x}$  (in frame {O}), what would its **transformation matrix** (i.e.  $T_O^T$ ) be for the same given value  $\theta^*$ ?

## 2. A Clean Take on Manipulation

[25 Points]



**Figure 1: A RP manipulator is used move a sponge to clean a curved surface**  
(Assume, if needed, that the robot base is placed at the centre of curvature of the surface)

A planar manipulator (Fig. 1) is used to move a sponge along a surface (S) for cleaning. For this arm, please:

- Establish and state a joint space ( $\mathbf{q}$ ) and workspace ( $\mathbf{W}$ ) for this arm
- Derive the forward kinematics of this arm (i.e.  $\mathbf{W} = f(\mathbf{q})$ )
- Derive the inverse kinematics of this arm (i.e.  $\mathbf{q} = g(\mathbf{W})$ )
- Derive the Jacobian matrix ( $\mathbf{J}$ ) associated with the coordinate transformation from joint displacements ( $\mathbf{q}$ ) to endpoint positions ( $\mathbf{W}$ ).
- The endpoint is required to move along the surface (S) at a constant velocity ( $\bar{\mathbf{C}} = \begin{bmatrix} c_1 \\ c_2 \end{bmatrix}$ ). **Please compute** the corresponding joint velocities in terms of the joint displacements and  $\bar{\mathbf{C}}$ .



### 3. Null Spaces Dualities

[10 Points]

- (a) What does the Null Space of the Jacobian ( $N(\mathbf{J})$ ) inform about Endpoint Velocities ( $\dot{\mathbf{x}}$ )?
- (b) What does the Null Space of the Transpose of the Jacobian ( $N(\mathbf{J}^T)$ ) inform about the Joint Torques ( $\boldsymbol{\tau}$ )?

## Part II: Sensing Kinematics

### 4. Getting Around the Hough Transform

[10 Points]

Please **briefly** explain the difference between the rectilinear and polar forms of the line Hough Transform. What is a **principle advantage** and **disadvantage** of using the polar form over the rectilinear form?

## 5. SNR: SIFT, Noise and Rotors!

[25 Points]



**Figure 2: An Aerial Image of the Florida Keys**

(Source: NOAA, Hurricane IRMA Imagery Dataset – <https://storms.ngs.noaa.gov/>)

Harvey, a video drone enthusiast, wants to make an aerial image (i.e. perform photogrammetry) of a region after a hurricane (such as the post-Irma Florida Keys). He proposes to use SIFT feature matching. To alleviate motion blur, he uses a downward-facing, high-frame rate camera.

- Can a SIFT feature descriptor exist without an initial “Harris corner” point?  
(if so, *why?*, if not, *why not?*)
- Because of the short exposure time (due to the high-frame rate), the pictures are corrupted by **moderate** levels of salt and pepper noise. Will SIFT matching still work?  
(Please briefly explain. If not, what can be done to make it work?)  
[Hint: How does SIFT achieve scale-invariance?]
- What constraints (*if any*) does the use of SIFT place on changes in **altitude** of the flight?  
(Please briefly explain.)
- What constraints (*if any*) does the use of SIFT place on changes in **attitude** (aerial vehicle orientation) of the flight?  
(Please briefly explain.)
- Can Harvey use a Quad-Rotor (i.e. an aerial vehicle that has cross-coupling between its roll, pitch and yaw and forward motion axes) to get the mosaic via SIFT?  
(Please briefly explain.)







6. Truth in Robotics!

[20 Points]

Please state if the following statements are generally **TRUE (T)** or **FALSE (F)**

(Kindly circle the answer  $\textcircled{T}$  or  $\textcircled{F}$ , a brief justification may be *optionally* added below)

- (a) If  $R \in SO(n)$ , then  $\det R = +1$  [ T | F ]
- (b) A 3R manipulator cannot be redundant in 3D space [ T | F ]
- (c) For a 3R planar arm having an overall Transformation Matrix ( ${}^oT^E$ ) from the origin  $\{O\}$  to the endpoint  $\{E\}$ , its inverse kinematics can be found directly from the inverse Transformation Matrix ( $T^{-1}$ ) [ T | F ]
- (d) A line is the axis of a pencil (one-parameter family) of planes [ T | F ]
- (e) A perspective transformation can map a sphere into a paraboloid [ T | F ]
- (f) As the focal length increases the effect of perspective is weaker [ T | F ]
- (g) The key idea in a Hough Transform is to map a (difficult) detection problem into a (simple) peak detection problem. [ T | F ]
- (h) If the colour of one object in the scene is known, then the colour can be normalized to it and then this colour can be used as a global feature. [ T | F ]
- (i) SIFT is **invariant** to small changes in lighting [ T | F ]
- (j) An edge detector often excels at finding corners [ T | F ]

