

30 Years of SLAM:

John Leonard

Samuel C. Collins Professor of Mechanical and Ocean Engineering
Massachusetts Institute of Technology

With thanks to many many people.....

30 Years of SLAM:

A Personal Historical Perspective
on 3 Decades of Mobile Robotics Research

John Leonard

Samuel C. Collins Professor of Mechanical and Ocean Engineering
Massachusetts Institute of Technology

With thanks to many many people.....

Outline

- 1985-2015
 - 30 Years of papers
 - Are the “old” questions answered?
 - How do we measure progress?
- Is SLAM “solved?”
 - If yes, how do we know it is solved?
 - If no, what are the open questions?

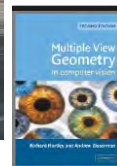
Q: Where am I?



Q: Where am I? A: Jenkin Building, Oxford



Q: Where am I? A: Jenkin Building, Oxford

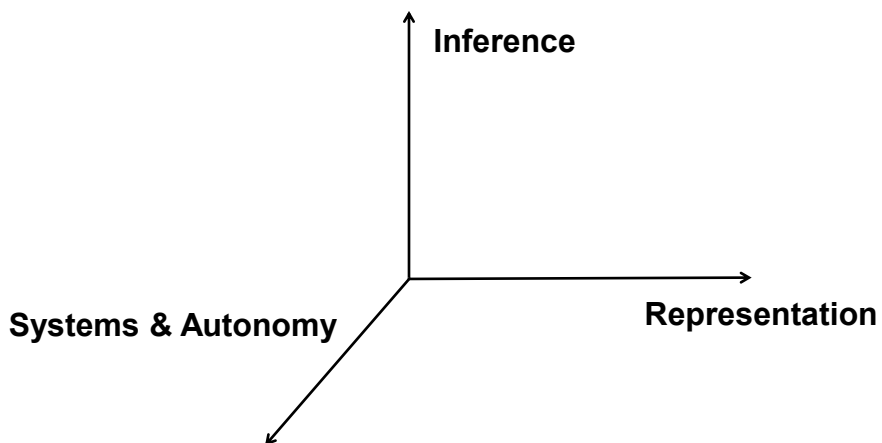


Hartley and Zisserman, Cambridge University Press

Jenkin Building Basement, Circa 1989



Why is SLAM Difficult?



Occupancy Grids

ICRA 1985

1985

High Resolution Maps from Wide Angle Sonar

Hans P. Moravec

Alberto Elfes

The Robotics Institute

Carnegie-Mellon University

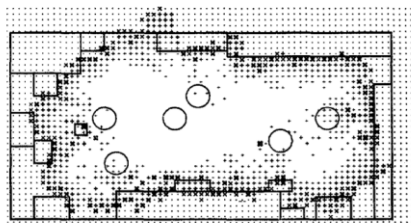
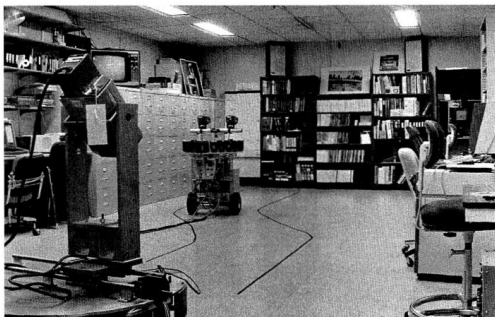


Figure 6: The Two-Dimensional Sonar Map After Thresholding.

Visual Map Making for a Mobile Robot

Rodney Brooks, ICRA 1985

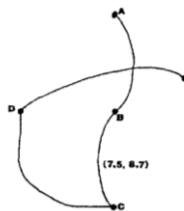
1985

Visual Map Making for a Mobile Robot

Rodney A. Brooks

MIT Artificial Intelligence Lab

545 Technology Square, Cambridge, Mass 02173.



Abstract. Mobile robots sense their environment and receive error laden readings. They try to move a certain distance and direction, and do so only approximately. Rather than try to engineer these problems away it may be possible, and may be necessary, to develop map making and navigation algorithms which explicitly represent these uncertainties, but still provide robust performance. The key idea is to use a relational map, which is rubbery and stretchy, rather than try to place observations in a 2-d coordinate system.

1. Introduction

We are interested in building mobile robot control systems useful for cheap robots (i.e., on the order of the price of an automobile) working in unstructured domains such as the home, material handling in factories, street cleaning, office and hotel cleaning, mining and agriculture. The same capabilities can be useful for robots, which do not have to be so cheap to be economically feasible, and which do tasks like: planetary exploration, space station maintenance and construction, asteroid mining, nuclear reactor operations, military reconnaissance and general military operations.

2. Almost all mobile robot projects have had as one of their underlying assumptions that it is desirable to produce a world model in an absolute coordinate system. However all sensors and control systems have both systematic and random errors. The former can be dealt with by calibration techniques (although these are often time consuming and are confounded on mobile robots by the fact that the robot itself is not fixed to any coordinate system). The latter are always present. It is usual to model some worse case bounds on such errors but this will not always suffice (e.g. mismatches in stereo vision can produce depth measurements with error magnitude the full range of depths which can be measured). In any case the bounded errors at least must be dealt with in building models of the world and using them. A number of approaches have been taken to this problem:

- Ignore it. This has only been successful in the most toylike of worlds.
- Use fixed reference beacons. This implies that the environment is either structured for the robot's benefit in the case that beacons are explicitly installed, or that the environment has been pre-surveyed for the robot's benefit in the case that known positions of existing beacons (e.g. power outlets) are used.

“The key idea is to use a relational map, which is rubbery and stretchy, rather than to try to place observations in a 2-D coordinate frame.

Position Referencing and Consistent World Modeling for Mobile Robots, ICRA 1985

1985

POSITION REFERENCING AND CONSISTENT WORLD MODELING FOR MOBILE ROBOTS *

Raja Chatila and Jean-Paul Laumond

Laboratoire d'Automatique et d'Analyse des Systemes du CNRS
7, Avenue du Colonel Roche 31077 Toulouse Cedex, France

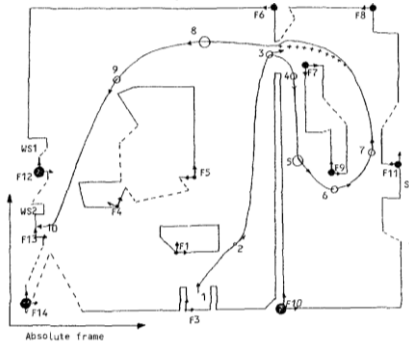


FIGURE 6: The final model with the associated errors on robot and frame position (the orientations errors are not represented)

French Television, 1982 **Chatila and Laumond, ICRA 1985**

A Stochastic Map for Spatial Relationships

1986

Smith, Self and Cheesemen

Proceedings of the Second Conference on Uncertainty in Artificial Intelligence, 1986

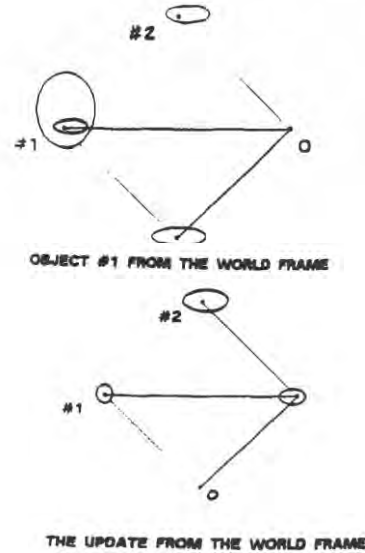
A Stochastic Map for Spatial Relationships

1986

Smith, Self and Cheesemen

Proceedings of the Second Conference on Uncertainty in Artificial Intelligence, 1986

“Rather than treat spatial uncertainty as a side issue in geometrical reasoning, we believe it must be an intrinsic part of spatial representations. In this paper, we describe a representation for spatial information, called the stochastic map, and associated procedures for building it, reading information from it, and revising it incrementally as new information is obtained.”

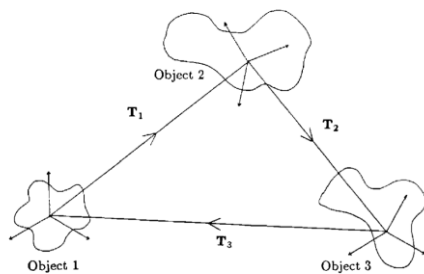


Consistent Integration and Propagation of Disparate Sensor Observations

1987

Hugh Durrant-Whyte

Fig. 1. Three objects in a relational loop.



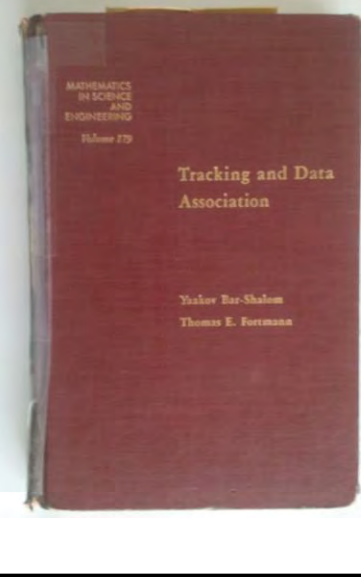
The International journal of robotics research 6 (3), 3-24



1988

Tracking and Data Association

Bar-Shalom and Fortmann, Academic Press, 1988

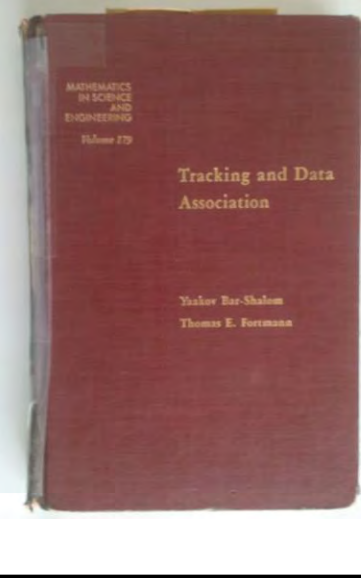
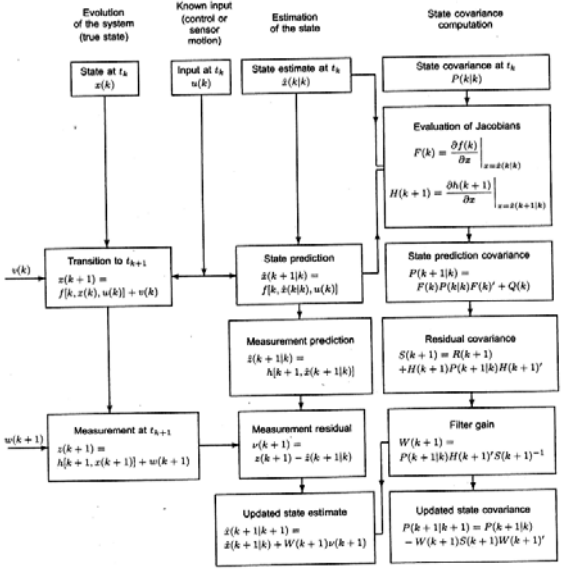


The image shows the front cover of the book 'Tracking and Data Association' by Yaakov Bar-Shalom and Thomas E. Fortmann, published in 1988. The cover is a dark red color with gold lettering. At the top, it says 'MATHEMATICS IN SCIENCE AND ENGINEERING' and 'Volume 179'. The title 'Tracking and Data Association' is prominently displayed in the center. Below the title, the authors' names 'Yaakov Bar-Shalom' and 'Thomas E. Fortmann' are listed.

1988

Tracking and Data Association

Bar-Shalom and Fortmann, Academic Press, 1988

The image shows the front cover of the book 'Tracking and Data Association' by Bar-Shalom and Fortmann, published in 1988, identical to the one above. To the right of the cover is a detailed flowchart of the Kalman filter algorithm, organized into four columns: Evolution of the system (true state), Known input (control or sensor motion), Estimation of the state, and State covariance computation.

Evolution of the system (true state):

- State at t_k : $x(k)$
- Transition to t_{k+1} : $x(k+1) = f[k, x(k), u(k)] + v(k)$
- Measurement at t_{k+1} : $z(k+1) = h[k+1, x(k+1)] + w(k+1)$

Known input (control or sensor motion):

- Input at t_k : $u(k)$

Estimation of the state:

- State estimate at t_k : $\hat{x}(k)$
- State prediction: $\hat{x}(k+1|k) = f[k, \hat{x}(k), u(k)]$
- Measurement prediction: $\hat{z}(k+1|k) = h[k+1, \hat{x}(k+1|k)]$
- Measurement residual: $v(k+1) = z(k+1) - \hat{z}(k+1|k)$
- Updated state estimate: $\hat{x}(k+1|k+1) = \hat{x}(k+1|k) + W(k+1)v(k+1)$

State covariance computation:

- State covariance at t_k : $P(k)$
- Evaluation of Jacobians: $F(k) = \left. \frac{\partial f(k)}{\partial x} \right|_{x=x(k)}$, $H(k+1) = \left. \frac{\partial h(k+1)}{\partial x} \right|_{x=x(k+1)}$
- State prediction covariance: $P(k+1|k) = F(k)P(k)F(k)' + Q(k)$
- Residual covariance: $S(k+1) = R(k+1) + H(k+1)P(k+1|k)H(k+1)'$
- Filter gain: $W(k+1) = P(k+1|k)H(k+1)'S(k+1)^{-1}$
- Updated state covariance: $P(k+1|k+1) = P(k+1|k) - W(k+1)S(k+1)W(k+1)'$

Localization with an *a priori* map 1990

Jenkin Building Basement, Oxford, 1990

Mapping from Known Locations 1990

The First Complete SLAM Implementation!

1991

The First Complete SLAM Implementation!
Philippe Moutarlier, LAAS

1991

Année 1991

THESE

présentée
 au Laboratoire d'Automatique et d'Analyse des Systèmes du CNRS
 en vue de l'obtention
 du Doctorat de l'Université Paul Sabatier de Toulouse
 Spécialité: Robotique

par
Philippe MOUTARLIER

**MODELISATION AUTONOME
 DE L'ENVIRONNEMENT
 PAR UN ROBOT MOBILE**

Soutenu le 18 Octobre 1991 devant le jury :

| | | |
|-----------|-------------|----------------|
| Georges | GIRALT | } Président |
| Nicholas | AYACHE | |
| Jean Paul | LAUMOND | } Rapporteurs |
| Bertrand | ZAVIDOVIQUE | |
| Maurice | BRIOT | } Examinateurs |
| Raja | CHATHA | |
| Roland | PRAJOUX | |
| Pierre | SOMMELET | |

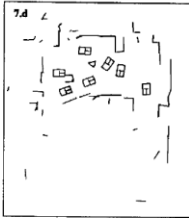




Figure 3.21 : A partir de maintenant les résultats vont différer suivant les méthodes. Nous finissons d'abord l'exploration et nous reviendrons sur ces différences.(Yaka)

Dynamic Environments (?)

1992

John J. Leonard
Hugh F. Durrant-Whyte
 Department of Engineering Science
 University of Oxford
 Parks Road, Oxford OX1 3PJ
 England

Ingemar J. Cox
 NEC Research Institute
 Princeton, New Jersey 08540

Dynamic Map Building for an Autonomous Mobile Robot

Abstract

This article presents an algorithm for autonomous map building and maintenance for a mobile robot. We believe that mobile robot navigation can be treated as a problem of tracking geometric features that occur naturally in the environment. We represent each feature in the map by a location estimate (the feature state vector) and two distinct measures of uncertainty: a covariance matrix to represent uncertainty in feature location, and a credibility measure to represent our belief in the validity of the feature. During each position update cycle, predicted measurements are generated for each geometric feature in the map and compared with actual sensor observations. Successful matches cause a feature's credibility to be increased. Unpredicted observations are used to initialize new geometric features, while unobserved predictions result in a geometric feature's credibility being decreased. We describe experimental results obtained with the algorithm that demonstrate successful map building using real sonar data.

IJRR, 1992

4 Simultaneous Localization and Map Building

The ideal localization system would allow the robot to start at a fixed location with no map of the surrounding environment, and from here to incrementally both build a map and use this map to locate its position relative to the start point. This is known as the simultaneous localization and map building (SLAM) problem. The SLAM problem is complex both as a mathematical exercise and in practical realization. It has received considerable attention over the years from a number of researchers [14, 5]. The essential problems are reasonably well known, however solutions have remained elusive, and a *significant* implementation has still not been attempted. We describe here the essential elements of the SLAM problem and some recent work in obtaining solutions to this problem.

1995

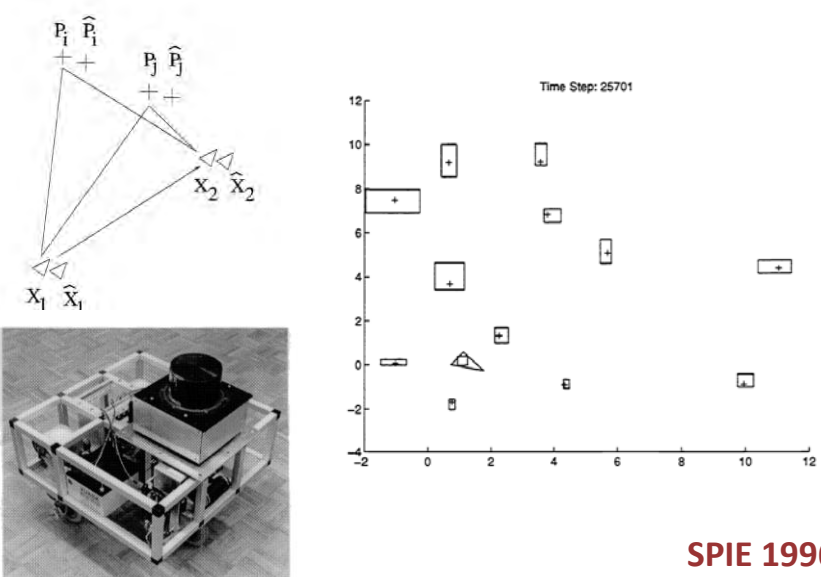
Hugh Durrant-Whyte
Grasp Lab PhD 1986

Advisor: Lou Paul
Mentors: Ruzena Bacjcsy and Max Mintz

Durrant-Whyte, et al., "Localization of Autonomous Guided Vehicles", ISRR, 1995

1996

New approach to simultaneous localization and dynamic map building. Csorba, Uhlmann, and Durrant-Whyte



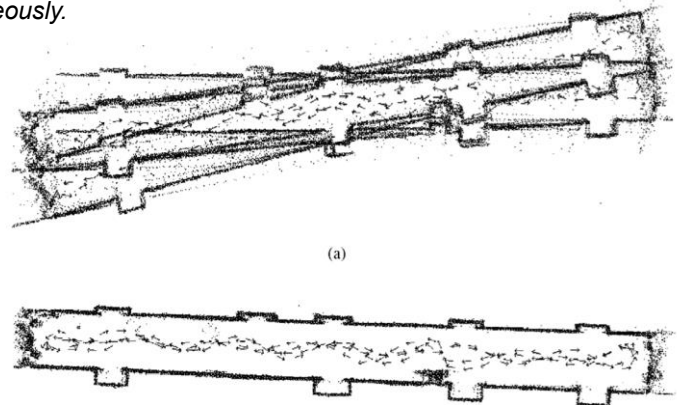
The diagram on the left shows a pose graph with nodes P_i, \hat{P}_i and P_j, \hat{P}_j connected to robot poses X_1, \hat{X}_1 and X_2, \hat{X}_2 . Below it is a photograph of a mobile robot. To the right is a 2D occupancy grid map at Time Step: 25701, showing a path with various symbols (crosses, squares, triangles) indicating robot positions and sensor measurements.

SPIE 1996

1997

Consistent Pose Estimation (Lu and Milios)

Our approach is to maintain all the local frames of data as well as the relative spatial relationships between local frames. These spatial relationships are modeled as random variables and are derived from matching pairwise scans or from odometry. Then we formulate a procedure based on the maximum likelihood criterion to optimally combine all the spatial relations. Consistency is achieved by using all the spatial relations as constraints to solve for the data frame poses simultaneously.




(a)

The figure shows two 2D occupancy grid maps of a hallway. The top map shows multiple overlapping scans from different robot poses, with lines connecting corresponding features across scans. The bottom map shows the resulting consistent pose estimation, where the scans are aligned and the robot's path is clearly visible.

Visual SLAM – Andrew Davison 1998


Mobile Robot Navigation Using Active Vision

Andrew John Davison
Keble College

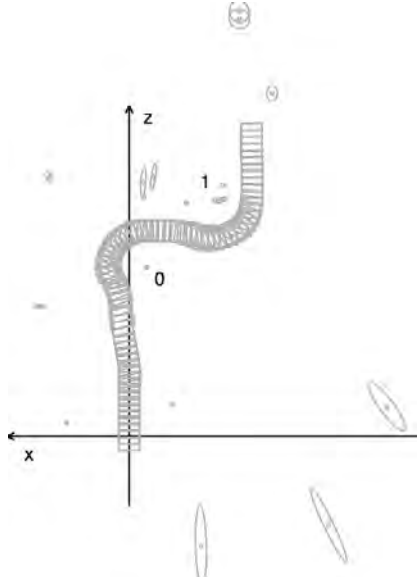

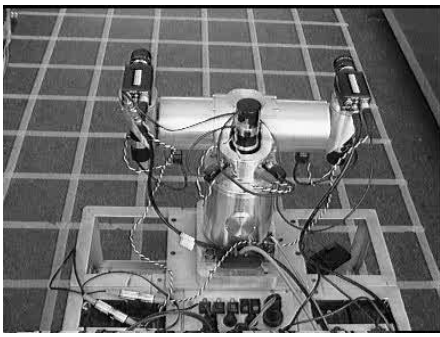


Robotics Research Group
Department of Engineering Science
University of Oxford

Submitted February 14 1998; Examined June 9th 1998.



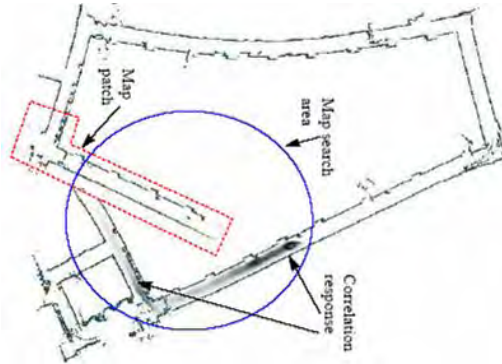
Visual SLAM – Andrew Davison 1998

1999

Loop-Closing – Gutmann and Konolige

“A map is represented as an undirected graph: nodes are robot poses with associated scans and links are constraints between poses obtained from dead-reckoning, scan-matching, or correlation (Gutmann and Konolige, CIRA, 1999)”



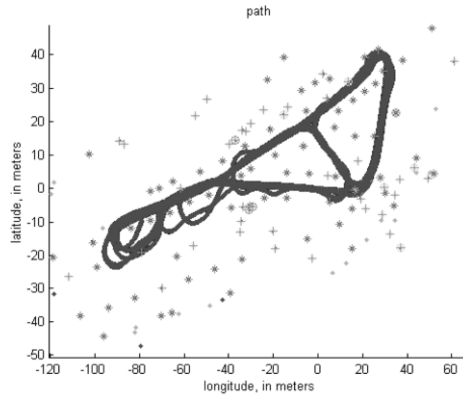
J.-S. Gutmann and K. Konolige. Incremental Mapping of Large Cyclic Environments, in: *International Symposium on Computational Intelligence in Robotics and Automation (CIRA'99)*, Monterey, November 1999.

2000

Probabilistic Algorithms and the Interactive Museum Tour-Guide Robot Minerva – Thrun et al.



Optimization of the Simultaneous Localization and Map Building Algorithm for Real Time Implementation (Guivant and Nebot) 2001



IEEE Trans R&A, 2001

Real-time SLAM using laser 2002
Paul Newman



Overhead view of scene (MIT Lobby 7)



Starting position



View from the robot



Real-time software



Return to home



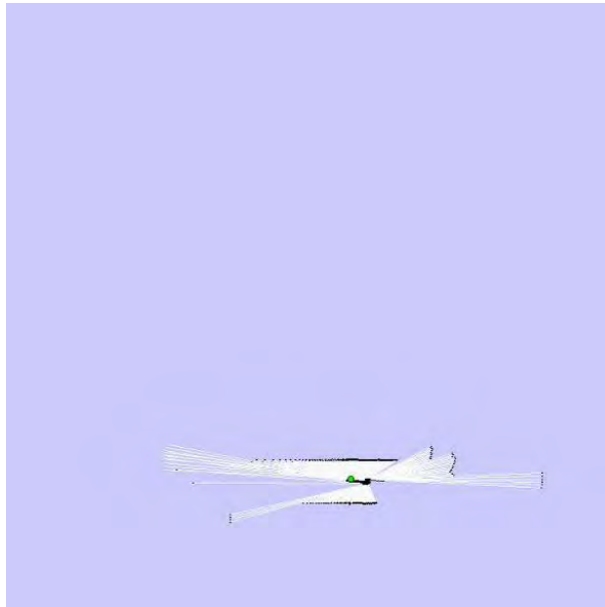
Final adjustment

First SLAM Summer School

2002

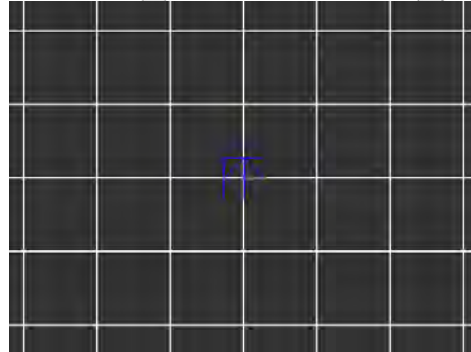
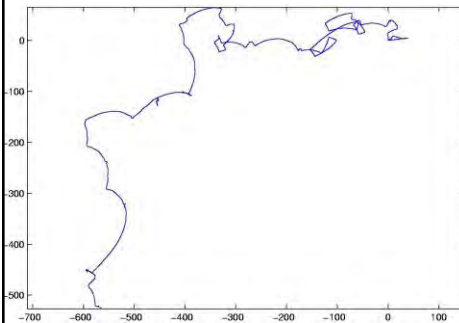
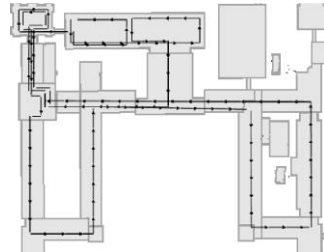
**Montemerlo and Thrun, FastSLAM**

2002



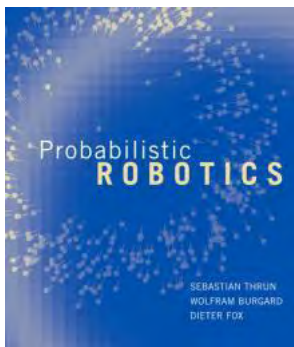
AAAI 2002 Video courtesy of Cyrill Stachniss (from several years later)

An Atlas Framework for Scalable Mapping (Bosse) 2003



ICRA 2003

Thrun, Burgard and Fox, MIT Press 2005



Wolfram Burgard, Dieter Fox and Sebastian Thrun (July, 2014)

Photo courtesy Wolfram Burgard

2006

Smoothing and Mapping (SAM) [Dellaert&Kaess, IJRR 06]

Graphical model

$$P(\mathbf{X} \mathbf{L} \mathbf{Z}) = P(x_1) \prod_{j=1}^{M-1} P(x_{j+1} | x_j, u_j) \prod_{k=1}^K P(z_k | x_{x_k}, l_{l_k})$$

negative log \downarrow linearize

Least-squares formulation:

$$\theta^* = \arg \min_{\theta} \|A\theta - b\|^2$$

Robot Poses

Landmarks

Measurement Jacobian

rhs

Incremental Smoothing and Mapping – Michael Kaess

12

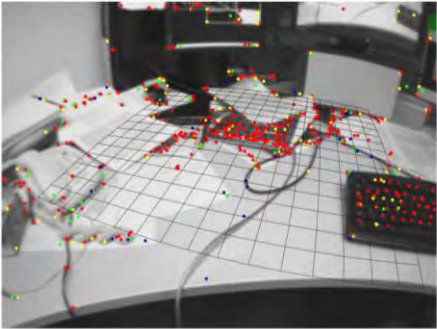
2007

G. Grisetti, C. Stachniss, S. Grzonka and W. Burgard A Tree Parameterization for Efficiently Computing Maximum Likelihood Maps using Gradient Descent

RSS 2007

2007

Parallel Tracking and Mapping (PTAM) **Klein and Murray**



Parallel Tracking and Mapping
for Small AR Workspaces


Extra video results made for
ISMAR 2007 conference

Georg Klein and David Murray
Active Vision Laboratory
University of Oxford

ISMAR, 2007 (Best Paper Award)

2009

FAB-MAP: Probabilistic Localization and Mapping in the Space of Appearance **Mark Cummins and Paul Newman**



New Place
 $p=1.0000$

IJRR 2009

Sibley et al. – Relative Bundle Adjustment/VSLAM

2010

Planes, Trains and Automobiles – Autonomy for the Modern Robot

Gabe Sibley, Christopher Mei, Ian Reid and Paul Newman



Abstract—We are concerned with enabling truly large scale autonomous navigation in typical human environments. To this end we describe the acquisition and modeling of large urban spaces from data that reflects human sensory input. Over 200GB of image and inertial data are captured using head-mounted stereo cameras. This data is processed into a relative map covering 121 km of Southern England. We point out the numerous challenges we encounter, and highlight in particular the problem of undetected ego-motion, which occurs when the robot finds itself on-or-within a moving frame of reference. In contrast to global-frame representations, we find that the continuous relative representation naturally accommodates moving-reference-frames – without having to identify them first, and without inconsistency. Within a moving-reference-frame, and without drift-less global exteroceptive sensing, motion with respect to the global-frame is effectively unobservable. This underlying truth drives us towards relative topometric solutions like relative bundle adjustment (RBA), which has no problem representing distance and metric Euclidean structure, yet does not suffer inconsistency introduced by the attempt to solve in the global-frame.

I. INTRODUCTION

Autonomous navigation in human working environments is an important problem, and this paper is motivated by our attempt to make sense of the 121 km path between Oxford and London depicted in Figs. 1 and 2. The map begins in an office in Oxford, and proceeds with various forms of transport



Figure 1: 121 km path between Oxford in the upper left and London in the bottom right. We compute visual estimates for 89.4% of this distance. Using appearance-based place recognition and inertial dead reckoning, 100% is covered topologically, which is sufficient for path planning. The graph begins in an office in Oxford, and proceeds with various forms of transport including: foot, bicycle, train, subway, escalator, rickshaw, punting-boat and ferris wheel. Note that we cannot detect our true position in the global inertial frame – when we are traveling on the train or subway for instance, motion with respect to the global inertial frame becomes effectively unobservable in the presence of noise.

ICRA 2010

KinectFusion – Izadi, Necombe et al.

2011

SIGGRAPH Talks 2011 KinectFusion: Real-Time Dynamic 3D Surface Reconstruction and Interaction

Shahram Izadi 1, Richard Newcombe 2, David Kim 1,3, Otmar Hilliges 1,
David Molyneaux 1,4, Pushmeet Kohli 1, Jamie Shotton 1,
Steve Hodges 1, Dustin Freeman 5, Andrew Davison 2, Andrew Fitzgibbon 1

1 Microsoft Research Cambridge 2 Imperial College London
3 Newcastle University 4 Lancaster University
5 University of Toronto

2012

Kintinuous (Whelan, McDonald et al.)

- Extension of KinectFusion (Newcombe, et al. ISMAR '11)
- Treat volumetric model as a cyclical buffer.
 - As region leaves the range of the buffer, extract surface data.
 - As region enters the range of the buffer, initialise and track the new data.

Whelan et al. RSS 2012 RGB-D Workshop

2013

SLAM++ Salas-Moreno et al.

**SLAM++ Demo
Imperial Festival 2013**

Renato Salas-Moreno
Richard Newcombe
Hauke Strasdat
Paul Kelly
Andrew Davison

Department of Computing
Imperial College London

CVPR 2013

Kintinous Processing Pipeline (“Cloud Slices” connected to pose graph SLAM optimization) 2013

Legend

1. Data move →
2. Conditional data move ⇄
3. Data store []
4. Function block []

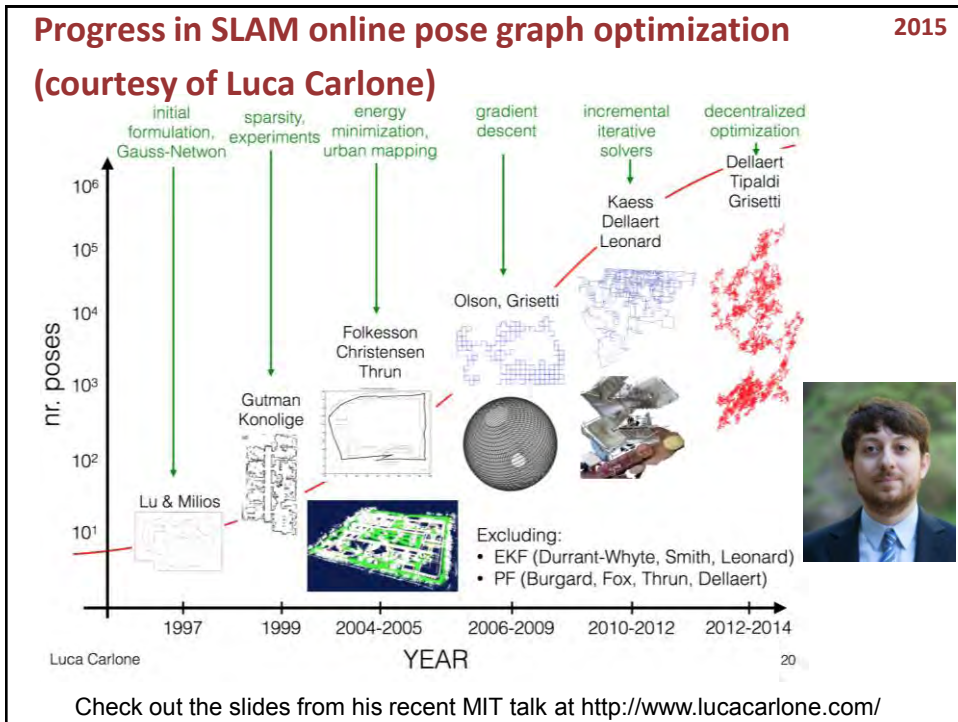
Function Name []

3D Visualizations:
 - TSDF Volume: Shows camera poses and TSDF slices.
 - Two slices: Shows a deformed slice. Text below: "Deformation @ 2,335,373 vertices, detection-to-correction latency: 5.78 seconds"

“Deformation-based Loop Closure for Large Scale Dense RGB-D SLAM” by
 T. Whelan, M. Kaess, J. Leonard and J. McDonald, IROS 2013

Google Tango – Journey 2014

www.youtube.com/watch?v=44vppay5UDc



Kintinuous with Stereo – Walking over Stairs 2015

Kintinuous with Dense Stereo on MIT DRC Atlas
 Maurice Fallon, Scott Kuidersma, Tom Whelan, and Russ Tedrake.

The figure consists of three parts:

- Top:** A photograph of a humanoid robot (Atlas) walking on a set of stairs in a laboratory setting.
- Bottom Left:** A group photograph of the researchers: Maurice Fallon, Scott Kuidersma, Tom Whelan, and Russ Tedrake.
- Bottom Right:** A 3D point cloud reconstruction of the stairs, showing the robot's path and the dense stereo data used for navigation.

Conclusion and Future Research Challenges

Goals:

- My dream is to achieve *persistent autonomy* and *lifelong map learning* in highly dynamic environments
- Can we robustly integrate mapping and localization with real-time planning and control?

Open Questions:

- Robustness – we would love to have guarantees of performance, but we do not have them for most approaches
- Representation – how can we integrate many different types?
- We need dynamic scene understanding and robust vision (recent work in computer vision is very exciting, but current precision-recall curves indicate we have a long way to go)

Is SLAM “Solved?”

Its an Exciting Time to Work in Mobile Sensing!

Postdocs and PhD students that can build real-time 3D perception, navigation and motion planning systems are in high demand:

- Virtual Reality
- Mobile Devices
- Self-Driving Vehicles
- Drones

Big tech companies such as Google, Apple, Facebook and Uber

Small startups such as skydio

Traditional companies in transition, such as Ford, Delphi, Continental, Bosch...

Vision for Mobile Robotics: A Research Agenda

- We need an *object-based* understanding of the environment that facilitates life-long learning
- Let's build rich representations that leverage knowledge of location to better understand about objects, and concurrently uses information about objects to better understand location
 - Sudeep Pillai: Monocular SLAM Supported Object Recognition (presented at RSS2015 on Tuesday)
 - Ross Finman: Automatic Discovery of Objects in lifelong Dense RGB-D maps
 - Key Idea: can we learn about objects through observing changes in the world?

Pillai and Leonard, RSS 2015**MONOCULAR SLAM SUPPORTED
OBJECT RECOGNITION**

Sudeep Pillai & John J. Leonard
Computer Science and Artificial Intelligence Lab
Massachusetts Institute of Technology

**Why is SLAM Difficult?**