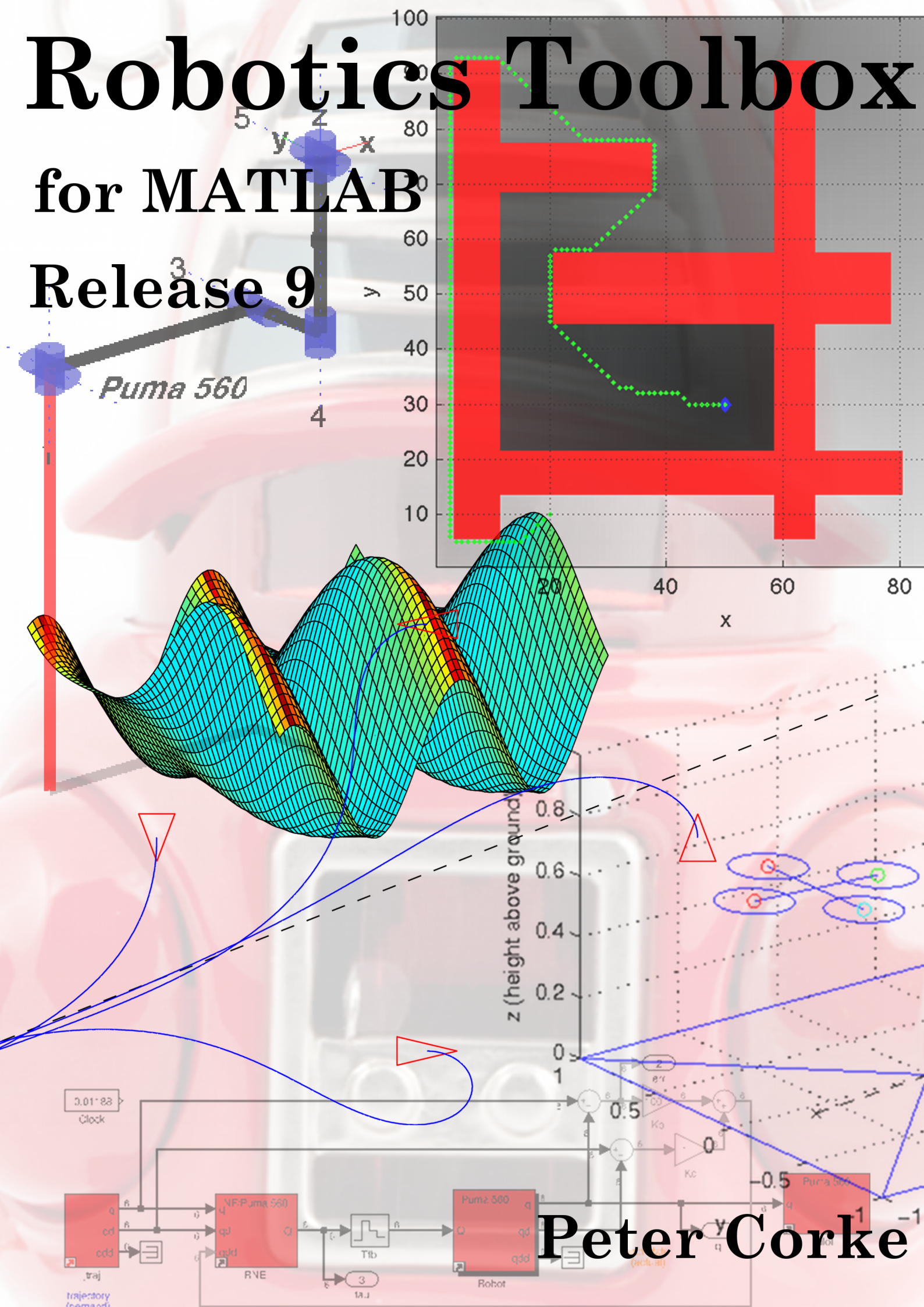
Robotics Toolbox

for MATLAB

Release 9



Peter Corke

Release	9.6
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Licence	LGPL
Toolbox home page	http://www.petercorke.com/robot
Discussion group	http://groups.google.com.au/group/robotics-tool-box

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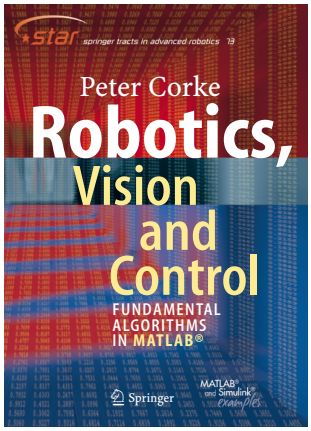
Preface



This, the ninth release of the Toolbox, represents over fifteen years of development and a substantial level of maturity. This version captures a large number of changes and extensions generated over the last two years which support my new book "*Robotics, Vision & Control*" shown to the left.

The Toolbox has always provided many functions that are useful for the study and simulation of classical arm-type robotics, for example such things as kinematics, dynamics, and trajectory generation. The Toolbox is based on a very general method of representing the kinematics and dynamics of serial-link manipulators. These parameters are encapsulated in MATLAB® objects — robot objects can be created by the user for any serial-link manipulator and a number of examples are provided for well know robots such as the Puma 560 and the Stanford arm amongst others. The Toolbox also provides functions for manipulating and converting between datatypes such as vectors, homogeneous transformations and unit-quaternions which are necessary to represent 3-dimensional position and orientation.

This ninth release of the Toolbox has been significantly extended to support mobile robots. For ground robots the Toolbox includes standard path planning algorithms (bug, distance transform, D*, PRM), kinodynamic planning (RRT), localization (EKF, particle filter), map building (EKF) and simultaneous localization and mapping (EKF), and a Simulink model a of non-holonomic vehicle. The Toolbox also including a detailed Simulink model for a quadcopter flying robot.

The routines are generally written in a straightforward manner which allows for easy understanding, perhaps at the expense of computational efficiency. If you feel strongly about computational efficiency then you can always rewrite the function to be more efficient, compile the M-file using the MATLAB® compiler, or create a MEX version.

The manual is now auto-generated from the comments in the MATLAB® code itself which reduces the effort in maintaining code and a separate manual as I used to — the downside is that there are no worked examples and figures in the manual. However the book "*Robotics, Vision & Control*" provides a detailed discussion (600 pages, nearly 400 figures and 1000 code examples) of how to use the Toolbox functions to solve

many types of problems in robotics, and I commend it to you.

Contents

Chapter 1

Introduction

1.1 What's changed

1.1.1 Documentation

- The manual (robot.pdf) no longer a separately written document. This was just too hard to keep updated with changes to code. All documentation is now in the m-file, making maintenance easier and consistency more likely. The negative consequence is that the manual is a little "drier" than it used to be.
- The Functions link from the Toolbox help browser lists all functions with hyperlinks to the individual help entries.
- Online HTML-format help is available from `http://www.petercorke.com/RTB/r9/html`

1.1.2 Changed behaviour

Compared to release 8 and earlier:

- The command `startup_rvc` should be executed before using the Toolbox. This sets up the MATLAB search paths correctly.
- The Robot class is now named SerialLink to be more specific.
- Almost all functions that operate on a SerialLink object are now methods rather than functions, for example plot() or fkine(). In practice this makes little difference to the user but operations can now be expressed as robot.plot(q) or plot(robot, q). Toolbox documentation now prefers the former convention which is more aligned with object-oriented practice.
- The parametrers to the Link object constructor are now in the order: theta, d, a, alpha. Why this order? It's the order in which the link transform is created: RZ(theta) TZ(d) TX(a) RX(alpha).
- All robot models now begin with the prefix mdl_, so puma560 is now mdl_puma560.

- The function drivebot is now the SerialLink method teach.
- The function ikine560 is now the SerialLink method ikine6s to indicate that it works for any 6-axis robot with a spherical wrist.
- The link class is now named Link to adhere to the convention that all classes begin with a capital letter.
- The `robot` class is now called `SerialLink`. It is created from a vector of `Link` objects, not a cell array.
- The quaternion class is now named Quaternion to adhere to the convention that all classes begin with a capital letter.
- A number of utility functions have been moved into the a directory common since they are not robot specific.
- skew no longer accepts a skew symmetric matrix as an argument and returns a 3-vector, this functionality is provided by the new function vex.
- tr2diff and diff2tr are now called tr2delta and delta2tr
- ctraj with a scalar argument now spaces the points according to a trapezoidal velocity profile (see lspb). To obtain even spacing provide a uniformly spaced vector as the third argument, eg. linspace(0, 1, N).
- The RPY functions tr2rpy and rpy2tr assume that the roll, pitch, yaw rotations are about the X, Y, Z axes which is consistent with common conventions for vehicles (planes, ships, ground vehicles). For some applications (eg. cameras) it useful to consider the rotations about the Z, Y, Z axes, and this behaviour can be obtained by using the option 'zyx' with these functions (note this is the pre release 8 behaviour).
- Many functions now accept MATLAB style arguments given as trailing strings, or string-value pairs. These are parsed by the internal function `tb_optparse`.

1.1.3 New functions

Release 9 introduces considerable new functionality, in particular for mobile robot control, navigation and localization:

- Mobile robotics:

  Vehicle Model of a mobile robot that has the "bicycle" kinematic model (car-like). For given inputs it updates the robot state and returns noise corrupted odometry measurements. This can be used in conjunction with a "driver" class such as RandomPath which drives the vehicle between random waypoints within a specified rectangular region.

  Sensor

  RangeBearingSensor Model of a laser scanner RangeBearingSensor, subclass of Sensor, that works in conjunction with a Map object to return range and bearing to invariant point features in the environment.

EKF Extended Kalman filter EKF can be used to perform localization by dead reckoning or map featuers, map buildings and simultaneous localization and mapping.

DXForm Path planning classes: distance transform DXform, D* lattice planner Dstar, probabilistic roadmap planner PRM, and rapidly exploring random tree RRT.

Monte Carlo estimator ParticleFilter.

- Arm robotics:

  jsingu

  jsingu

  qplot

  DHFactor a simple means to generate the Denavit-Hartenberg kinematic model of a robot from a sequence of elementary transforms.

- Trajectory related:

  lspb

  tpoly

  mtraj

  mstraj

- General transformation:

  wtrans

  se2

  se3

  homtrans

  vex performs the inverse function to skew, it converts a skew-symmetric matrix to a 3-vector.

- Data structures:

  Pgraph represents a non-directed embedded graph, supports plotting and minimum cost path finding.

  Polygon a generic 2D polygon class that supports plotting, intersectio/union/difference of polygons, line/polygon intersection, point/polygon containment.

- Graphical functions:

  trprint compact display of a transform in various formats.

  trplot display a coordinate frame in SE(3)

  trplot2 as above but for SE(2)

  tranimate animate the motion of a coordinate frame

plot_box plot a box given TL/BR corners or center+WH, with options for edge color, fill color and transparency.

plot_circle plot one or more circles, with options for edge color, fill color and transparency.

plot_sphere plot a sphere, with options for edge color, fill color and transparency.

plot_ellipse plot an ellipse, with options for edge color, fill color and transparency.

]plot_ellipsoid] plot an ellipsoid, with options for edge color, fill color and transparency.

plot_poly plot a polygon, with options for edge color, fill color and transparency.

- Utility:

  about display a one line summary of a matrix or class, a compact version of whos

  tb_optparse general argument handler and options parser, used internally in many functions.

- Lots of Simulink models are provided in the subdirectory `simulink`. These models all have the prefix `sl_`.

1.1.4 Improvements

- Many functions now accept MATLAB style arguments given as trailing strings, or string-value pairs. These are parsed by the internal function `tb_optparse`.
- Many functions now handle sequences of rotation matrices or homogeneous transformations.
- Improved error messages in many functions
- Removed trailing commas from if and for statements

1.2 How to obtain the Toolbox

The Robotics Toolbox is freely available from the Toolbox home page at

`http://www.petercorke.com`

The files are available in zip format (.zip). The web page requests some information from you such as your country, type of organization and application. This is just a means for me to gauge interest and to help convince my bosses (and myself) that this is a worthwhile activity.

The file `robot.pdf` is a manual that describes all functions in the Toolbox. It is auto-generated from the comments in the MATLAB® code and is fully hyperlinked:

to external web sites, the table of content to functions, and the "See also" functions to each other.

A menu-driven demonstration can be invoked by the function `rtdemo`.

1.3 MATLAB version issues

The Toolbox has been tested under R2011a.

1.4 Use in teaching

This is definitely encouraged! You are free to put the PDF manual (`robot.pdf` or the web-based documentation `html/*.html` on a server for class use. If you plan to distribute paper copies of the PDF manual then every copy must include the first two pages (cover and licence).

1.5 Use in research

If the Toolbox helps you in your endeavours then I'd appreciate you citing the Toolbox when you publish. The details are

```
@ARTICLE{Corke96b,
        AUTHOR              = {P.I. Corke},
        JOURNAL             = {IEEE Robotics and Automation Magazine},
        MONTH               = mar,
        NUMBER              = {1},
        PAGES               = {24-32},
        TITLE               = {A Robotics Toolbox for {MATLAB}},
        VOLUME              = {3},
        YEAR                = {1996}
}
```

or

> "*A robotics toolbox for MATLAB*",
> P.Corke,
> IEEE Robotics and Automation Magazine,
> vol.3, pp.2432, Sept. 1996.

which is also given in electronic form in the README file.

1.6 Support

There is no support! This software is made freely available in the hope that you find it useful in solving whatever problems you have to hand. I am happy to correspond

with people who have found genuine bugs or deficiencies but my response time can be long and I can't guarantee that I respond to your email. I am very happy to accept contributions for inclusion in future versions of the toolbox, and you will be suitably acknowledged.

I can guarantee that I will not respond to any requests for help with assignments or homework, no matter how urgent or important they might be to you. That's what you your teachers, tutors, lecturers and professors are paid to do.

You might instead like to communicate with other users via the Google Group called "Robotics and Machine Vision Toolbox"

http://groups.google.com.au/group/robotics-tool-box

which is a forum for discussion. You need to signup in order to post, and the signup process is moderated by me so allow a few days for this to happen. I need you to write a few words about why you want to join the list so I can distinguish you from a spammer or a web-bot.

1.7 Related software

1.7.1 Octave

Octave is an open-source mathematical environment that is very similar to MATLAB®, but it has some important differences particularly with respect to graphics and classes. Many Toolbox functions work just fine under Octave. Three important classes (Quaternion, Link and SerialLink) will not work so modified versions of these classes is provided in the subdirectory called `Octave`. Copy all the directories from `Octave` to the main Robotics Toolbox directory.

The Octave port is a second priority for support and upgrades and is offered in the hope that you find it useful.

1.7.2 Python version

A python implementation of the Toolbox at http://code.google.com/p/robotics-toolbox-python. All core functionality of the release 8 Toolbox is present including kinematics, dynamics, Jacobians, quaternions etc. It is based on the python numpy class. The main current limitation is the lack of good 3D graphics support but people are working on this. Nevertheless this version of the toolbox is very usable and of course you don't need a MATLAB® licence to use it. Watch this space.

1.7.3 Machine Vision toolbox

Machine Vision toolbox (MVTB) for MATLAB®. This was described in an article

```
@article{Corke05d,
        Author = {P.I. Corke},
        Journal = {IEEE Robotics and Automation Magazine},
```



```
        Month = nov,
        Number = {4},
        Pages = {16-25},
        Title = {Machine Vision Toolbox},
        Volume = {12},
        Year = {2005}}
```

and provides a very wide range of useful computer vision functions beyond the Mathwork's Image Processing Toolbox. You can obtain this from http://www.petercorke.com/vision.

1.8 Acknowledgements

Last, but not least, I have corresponded with a great many people via email since the first release of this Toolbox. Some have identified bugs and shortcomings in the documentation, and even better, some have provided bug fixes and even new modules, thankyou. See the file CONTRIB for details. I'd like to especially mention Wynand Smart for some arm robot models, Paul Pounds for the quadcopter model, and Paul Newman (Oxford) for inspiring the mobile robot code.

Chapter 2

Functions and classes

about

Compact display of variable type

about(**x**) displays a compact line that describes the class and dimensions of **x**.

about **x** as above but this is the command rather than functional form

See also

whos

---

angdiff

Difference of two angles

d = **angdiff**(**th1**, **th2**) returns the difference between angles **th1** and **th2** on the circle. The result is in the interval [-pi pi). If **th1** is a column vector, and **th2** a scalar then return a column vector where **th2** is modulo subtracted from the corresponding elements of **th1**.

d = **angdiff**(**th**) returns the equivalent angle to **th** in the interval [-pi pi).

Return the equivalent angle in the interval [-pi pi).

---

angvec2r

Convert angle and vector orientation to a rotation matrix

R = **angvec2r**(**theta**, **v**) is an rthonormal rotation matrix, **R**, equivalent to a rotation of **theta** about the vector **v**.

See also

eul2r, rpy2r

---

angvec2tr

Convert angle and vector orientation to a homogeneous transform

T = **angvec2tr**(**theta**, **v**) is a homogeneous transform matrix equivalent to a rotation of **theta** about the vector **v**.

Note

- The translational part is zero.

See also

eul2tr, rpy2tr, angvec2r

---

bresenham

Generate a line

p = **bresenham**(**x1**, **y1**, **x2**, **y2**) is a list of integer coordinates for points lying on the line segement (**x1**,**y1**) to (**x2**,**y2**). Endpoints must be integer.

p = **bresenham**(**p1**, **p2**) as above but **p1**=[**x1**,**y1**] and **p2**=[**x2**,**y2**].

See also

icanvas

Bug2

Bug navigation class

A concrete subclass of the Navigation class that implements the bug2 navigation algorithm. This is a simple automaton that performs local planning, that is, it can only sense the immediate presence of an obstacle.

Methods

path	Compute a path from start to goal
visualize	Display the obstacle map (deprecated)
plot	Display the obstacle map
display	Display state/parameters in human readable form
char	Convert to string

Example

```
load map1            % load the map
bug = Bug2(map);     % create navigation object

 bug.goal = [50, 35];  % set the goal

bug.path([20, 10]);    % animate path to (20,10)
```

Reference

- Dynamic path planning for a mobile automaton with limited information on the environment,, V. Lumelsky and A. Stepanov, IEEE Transactions on Automatic Control, vol. 31, pp. 1058-1063, Nov. 1986.
- Robotics, Vision & Control, Sec 5.1.2, Peter Corke, Springer, 2011.

See also

Navigation, DXform, Dstar, PRM

Bug2.Bug2

bug2 navigation object constructor

b = Bug2(**map**) is a bug2 navigation object, and **map** is an occupancy grid, a representation of a planar world as a matrix whose elements are 0 (free space) or 1 (occupied).

Options

'goal', G	Specify the goal point (1×2)
'inflate', K	Inflate all obstacles by K cells.

See also

Navigation.Navigation

---

circle

Compute points on a circle

circle(**C**, **R**, **opt**) plot a circle centred at **C** with radius **R**.

x = circle(**C**, **R**, **opt**) return an $N \times 2$ matrix whose rows define the coordinates [x,y] of points around the circumferance of a circle centred at **C** and of radius **R**.

C is normally 2×1 but if 3×1 then the circle is embedded in 3D, and **x** is $N \times 3$, but the circle is always in the xy-plane with a z-coordinate of **C**(3).

Options

'n', N	Specify the number of points (default 50)

---

colnorm

Column-wise norm of a matrix

cn = colnorm(**a**) is an $M \times 1$ vector of the normals of each column of the matrix **a** which is $N \times M$.

ctraj

Cartesian trajectory between two points

tc = **ctraj**(**T0**, **T1**, **n**) is a Cartesian trajectory ($4 \times 4 \times$ **n**) from pose **T0** to **T1** with **n** points that follow a trapezoidal velocity profile along the path. The Cartesian trajectory is a homogeneous transform sequence and the last subscript being the point index, that is, T(:,:,i) is the i'th point along the path.

tc = **ctraj**(**T0**, **T1**, **s**) as above but the elements of **s** (**n** $\times$ 1) specify the fractional distance along the path, and these values are in the range [0 1]. The i'th point corresponds to a distance **s**(i) along the path.

See also

lspb, mstraj, trinterp, Quaternion.interp, transl

delta2tr

Convert differential motion to a homogeneous transform

T = **delta2tr**(**d**) is a homogeneous transform representing differential translation and rotation. The vector **d**=(dx, dy, dz, dRx, dRy, dRz) represents an infinitessimal motion, and is an approximation to the spatial velocity multiplied by time.

See also

tr2delta

DHFactor

Simplify symbolic link transform expressions

f = **dhfactor**(**s**) is an object that encodes the kinematic model of a robot provided by a string **s** that represents a chain of elementary transforms from the robot's base to its

tool tip. The chain of elementary rotations and translations is symbolically factored into a sequence of link transforms described by DH parameters.

For example:

```
s = 'Rz(q1).Rx(q2).Ty(L1).Rx(q3).Tz(L2)';
```

indicates a rotation of q1 about the z-axis, then rotation of q2 about the x-axis, translation of L1 about the y-axis, rotation of q3 about the x-axis and translation of L2 along the z-axis.

Methods

base	the base transform as a Java string
tool	the tool transform as a Java string
command	a command string that will create a SerialLink() object representing the specified kinematics
char	convert to string representation
display	display in human readable form

Example

```
>> s = 'Rz(q1).Rx(q2).Ty(L1).Rx(q3).Tz(L2)';
>> dh = DHFactor(s);
>> dh
DH(q1+90, 0, 0, +90).DH(q2, L1, 0, 0).DH(q3-90, L2, 0, 0).Rz(+90).Rx(-90).Rz(-90)
>> r = eval( dh.command('myrobot') );
```

Notes

- Variables starting with q are assumed to be joint coordinates
- Variables starting with L are length constants.
- Length constants must be defined in the workspace before executing the last line above.
- Implemented in Java
- Not all sequences can be converted to DH format, if conversion cannot be achieved an error is generated.

Reference

- A simple and systematic approach to assigning Denavit-Hartenberg parameters, P.Corke, IEEE Transaction on Robotics, vol. 23, pp. 590-594, June 2007.
- Robotics, Vision & Control, Sec 7.5.2, 7.7.1, Peter Corke, Springer 2011.

See also

SerialLink

---

diff2

Two point difference

d = **diff2**(**v**) is the 2-point difference for each point in the vector v and the first element is zero. The vector **d** has the same length as **v**.

See also

diff

---

distancexform

Distance transform of occupancy grid

d = **distancexform**(**world**, **goal**) is the distance transform of the occupancy grid **world** with respect to the specified goal point **goal** = [X,Y]. The elements of the grid are 0 from free space and 1 for occupied.

d = **distancexform**(**world**, **goal**, **metric**) as above but specifies the distance metric as either 'cityblock' or 'Euclidean'

d = **distancexform**(**world**, **goal**, **metric**, **show**) as above but shows an animation of the distance transform being formed, with a delay of **show** seconds between frames.

Notes

- The Machine Vision Toolbox function imorph is required.
- The goal is [X,Y] not MATLAB [row,col]

See also

imorph, DXform

Dstar

D* navigation class

A concrete subclass of the Navigation class that implements the D* navigation algorithm. This provides minimum distance paths and facilitates incremental replanning.

Methods

plan	Compute the cost map given a goal and map
path	Compute a path to the goal
visualize	Display the obstacle map (deprecated)
plot	Display the obstacle map
costmap_modify	Modify the costmap
modify_cost	Modify the costmap (deprecated, use costmap_modify)
costmap_get	Return the current costmap
costmap_set	Set the current costmap
distancemap_get	Set the current distance map
display	Print the parameters in human readable form
char	Convert to string

Properties

costmap	Distance from each point to the goal.

Example

```
load map1           % load map
goal = [50,30];
start=[20,10];
ds = Dstar(map);    % create navigation object
ds.plan(goal)       % create plan for specified goal
ds.path(start)      % animate path from this start location
```

Notes

- Obstacles are represented by Inf in the costmap.

- The value of each element in the costmap is the shortest distance from the corresponding point in the map to the current goal.

References

- The D* algorithm for real-time planning of optimal traverses, A. Stentz, Tech. Rep. CMU-RI-TR-94-37, The Robotics Institute, Carnegie-Mellon University, 1994.
- Robotics, Vision & Control, Sec 5.2.2, Peter Corke, Springer, 2011.

See also

Navigation, DXform, PRM

Dstar.Dstar

D* constructor

ds = **Dstar**(**map**, **options**) is a D* navigation object, and **map** is an occupancy grid, a representation of a planar world as a matrix whose elements are 0 (free space) or 1 (occupied). The occupancy grid is coverted to a costmap with a unit cost for traversing a cell.

Options

'goal', G	Specify the goal point (2×1)
'metric', M	Specify the distance metric as 'euclidean' (default) or 'cityblock'.
'inflate', K	Inflate all obstacles by K cells.
'quiet'	Don't display the progress spinner

Other options are supported by the Navigation superclass.

See also

Navigation.Navigation

Dstar.char

Convert navigation object to string

DS.**char**() is a string representing the state of the **Dstar** object in human-readable form.

See also

Dstar.display, Navigation.char

Dstar.costmap_get

Get the current costmap

C = DS.costmap_get() is the current costmap. The cost map is the same size as the occupancy grid and the value of each element represents the cost of traversing the cell. It is autogenerated by the class constructor from the occupancy grid such that:

- free cell (occupancy 0) has a cost of 1
- occupied cell (occupancy >0) has a cost of Inf

See also

Dstar.costmap_set, Dstar.costmap_modify

Dstar.costmap_modify

Modify cost map

DS.costmap_modify(**p**, **new**) modifies the cost map at **p**=[X,Y] to have the value **new**. If **p** $(2 \times M)$ and **new** $(1 \times M)$ then the cost of the points defined by the columns of **p** are set to the corresponding elements of **new**.

Notes

- After one or more point costs have been updated the path should be replanned by calling DS.plan().
- Replaces modify_cost, same syntax.

See also

Dstar.costmap_set, Dstar.costmap_get

Dstar.costmap_set

Set the current costmap

DS.costmap_set(**C**) sets the current costmap. The cost map is the same size as the occupancy grid and the value of each element represents the cost of traversing the cell. A high value indicates that the cell is more costly (difficult) to traverese. A value of Inf indicates an obstacle.

Notes

- After the cost map is changed the path should be replanned by calling DS.plan().

See also

Dstar.costmap_get, Dstar.costmap_modify

Dstar.distancemap_get

Get the current distance map

C = DS.distancemap_get() is the current distance map. This map is the same size as the occupancy grid and the value of each element is the shortest distance from the corresponding point in the map to the current goal. It is computed by **Dstar**.plan.

See also

Dstar.plan

Dstar.modify_cost

Modify cost map

Notes

- Deprecated: use modify_cost instead instead.

See also

Dstar.costmap_set, Dstar.costmap_get

Dstar.plan

Plan path to goal

DS.**plan**() updates DS with a costmap of distance to the goal from every non-obstacle point in the map. The goal is as specified to the constructor.

DS.**plan**(**goal**) as above but uses the specified goal.

Note

- If a path has already been planned, but the costmap was modified, then reinvoking this method will replan, incrementally updating the **plan** at lower cost than a full replan.

Dstar.plot

Visualize navigation environment

DS.**plot**() displays the occupancy grid and the goal distance in a new figure. The goal distance is shown by intensity which increases with distance from the goal. Obstacles are overlaid and shown in red.

DS.**plot**(**p**) as above but also overlays a path given by the set of points **p** ($M \times 2$).

See also

Navigation.plot

Dstar.reset

Reset the planner

DS.**reset**() resets the D* planner. The next instantiation of DS.plan() will perform a global replan.

DXform

Distance transform navigation class

A concrete subclass of the Navigation class that implements the distance transform navigation algorithm which computes minimum distance paths.

Methods

plan	Compute the cost map given a goal and map
path	Compute a path to the goal
visualize	Display the obstacle map (deprecated)
plot	Display the distance function and obstacle map
plot3d	Display the distance function as a surface
display	Print the parameters in human readable form
char	Convert to string

Properties

distancemap	The distance transform of the occupancy grid.
metric	The distance metric, can be 'euclidean' (default) or 'cityblock'

Example

```
load map1           % load map
goal = [50,30];     % goal point
start = [20, 10];   % start point
dx = DXform(map);   % create navigation object
dx.plan(goal)       % create plan for specified goal
dx.path(start)      % animate path from this start location
```

Notes

- Obstacles are represented by NaN in the distancemap.
- The value of each element in the distancemap is the shortest distance from the corresponding point in the map to the current goal.

References

- Robotics, Vision & Control, Sec 5.2.1, Peter Corke, Springer, 2011.

See also

Navigation, Dstar, PRM, distancexform

DXform.DXform

Distance transform constructor

dx = DXform(map, options) is a distance transform navigation object, and **map** is an occupancy grid, a representation of a planar world as a matrix whose elements are 0 (free space) or 1 (occupied).

Options

'goal', G	Specify the goal point (2×1)
'metric', M	Specify the distance metric as 'euclidean' (default) or 'cityblock'.
'inflate', K	Inflate all obstacles by K cells.

Other options are supported by the Navigation superclass.

See also

Navigation.Navigation

DXform.char

Convert to string

DX.**char**() is a string representing the state of the object in human-readable form.

See also **DXform**.display, Navigation.**char**

DXform.plan

Plan path to goal

DX.**plan**() updates the internal distancemap where the value of each element is the minimum distance from the corresponding point to the goal. The goal is as specified to the constructor.

DX.**plan**(**goal**) as above but uses the specified goal.

DX.**plan**(**goal**, **s**) as above but displays the evolution of the distancemap, with one iteration displayed every **s** seconds.

Notes

- This may take many seconds.

DXform.plot

Visualize navigation environment

DX.**plot**() displays the occupancy grid and the goal distance in a new figure. The goal distance is shown by intensity which increases with distance from the goal. Obstacles are overlaid and shown in red.

DX.**plot**(**p**) as above but also overlays a path given by the set of points **p** ($M \times 2$).

See also

Navigation.plot

DXform.plot3d

3D costmap view

DX.**plot3d**() displays the distance function as a 3D surface with distance from goal as the vertical axis. Obstacles are "cut out" from the surface.

DX.**plot3d**(**p**) as above but also overlays a path given by the set of points **p** ($M \times 2$).

DX.**plot3d**(**p**, **ls**) as above but plot the line with the linestyle **ls**.

See also

Navigation.plot

---

e2h

Euclidean to homogeneous

H = e2h(**E**) is the homogeneous version (K+1 $\times$ N) of the Euclidean points **E** ($K \times N$) where each column represents one point in R^K.

See also

h2e

EKF

Extended Kalman Filter for navigation

This class can be used for:

- dead reckoning localization
- map-based localization
- map making
- simultaneous localization and mapping (SLAM)

It is used in conjunction with:

- a kinematic vehicle model that provides odometry output, represented by a Vehicle object.
- The vehicle must be driven within the area of the map and this is achieved by connecting the Vehicle object to a Driver object.
- a map containing the position of a number of landmark points and is represented by a Map object.
- a sensor that returns measurements about landmarks relative to the vehicle's location and is represented by a Sensor object subclass.

The EKF object updates its state at each time step, and invokes the state update methods of the Vehicle. The complete history of estimated state and covariance is stored within the EKF object.

Methods

run	run the filter
plot_xy	plot the actual path of the vehicle
plot_P	plot the estimated covariance norm along the path
plot_map	plot estimated feature points and confidence limits
plot_ellipse	plot estimated path with covariance ellipses
display	print the filter state in human readable form
char	convert the filter state to human readable string

Properties

x_est	estimated state
P	estimated covariance
V_est	estimated odometry covariance
W_est	estimated sensor covariance
features	maps sensor feature id to filter state element
robot	reference to the Vehicle object
sensor	reference to the Sensor subclass object
history	vector of structs that hold the detailed filter state from each time step
verbose	show lots of detail (default false)
joseph	use Joseph form to represent covariance (default true)

Vehicle position estimation (localization)

Create a vehicle with odometry covariance V, add a driver to it, create a Kalman filter with estimated covariance V_est and initial state covariance P0

```
veh = Vehicle(V);
veh.add_driver( RandomPath(20, 2) );
ekf = EKF(veh, V_est, P0);
```

We run the simulation for 1000 time steps

```
ekf.run(1000);
```

then plot true vehicle path

```
veh.plot_xy('b');
```

and overlay the estimated path

```
ekf.plot_xy('r');
```

and overlay uncertainty ellipses at every 20 time steps

```
ekf.plot_ellipse(20, 'g');
```

We can plot the covariance against time as

```
clf
ekf.plot_P();
```


Map-based vehicle localization

Create a vehicle with odometry covariance V, add a driver to it, create a map with 20 point features, create a sensor that uses the map and vehicle state to estimate feature range and bearing with covariance W, the Kalman filter with estimated covariances V_est and W_est and initial vehicle state covariance P0

```
veh = Vehicle(V);
veh.add_driver( RandomPath(20, 2) );
map = Map(20);
sensor = RangeBearingSensor(veh, map, W);
ekf = EKF(veh, V_est, P0, sensor, W_est, map);
```

We run the simulation for 1000 time steps

```
ekf.run(1000);
```

then plot the map and the true vehicle path

```
map.plot();
veh.plot_xy('b');
```

and overlay the estimatd path

```
ekf.plot_xy('r');
```

and overlay uncertainty ellipses at every 20 time steps

```
ekf.plot_ellipse([], 'g');
```

We can plot the covariance against time as

```
clf
ekf.plot_P();
```

Vehicle-based map making

Create a vehicle with odometry covariance V, add a driver to it, create a sensor that uses the map and vehicle state to estimate feature range and bearing with covariance W, the Kalman filter with estimated sensor covariance W_est and a "perfect" vehicle (no covariance), then run the filter for N time steps.

```
veh = Vehicle(V);
veh.add_driver( RandomPath(20, 2) );
sensor = RangeBearingSensor(veh, map, W);
ekf = EKF(veh, [], [], sensor, W_est, []);
```

We run the simulation for 1000 time steps

```
ekf.run(1000);
```

Then plot the true map

```
map.plot();
```

and overlay the estimated map with 3 sigma ellipses

```
ekf.plot_map(3, 'g');
```


Simultaneous localization and mapping (SLAM)

Create a vehicle with odometry covariance V, add a driver to it, create a map with 20 point features, create a sensor that uses the map and vehicle state to estimate feature range and bearing with covariance W, the Kalman filter with estimated covariances V_est and W_est and initial state covariance P0, then run the filter to estimate the vehicle state at each time step and the map.

```
veh = Vehicle(V);
veh.add_driver( RandomPath(20, 2) );
map = Map(20);
sensor = RangeBearingSensor(veh, map, W);
ekf = EKF(veh, V_est, P0, sensor, W, []);
```

We run the simulation for 1000 time steps

```
ekf.run(1000);
```

then plot the map and the true vehicle path

```
map.plot();
veh.plot_xy('b');
```

and overlay the estimated path

```
ekf.plot_xy('r');
```

and overlay uncertainty ellipses at every 20 time steps

```
ekf.plot_ellipse([], 'g');
```

We can plot the covariance against time as

```
clf
ekf.plot_P();
```

Then plot the true map

```
map.plot();
```

and overlay the estimated map with 3 sigma ellipses

```
ekf.plot_map(3, 'g');
```

Reference

Robotics, Vision & Control, Chap 6, Peter Corke, Springer 2011

Acknowledgement

Inspired by code of Paul Newman, Oxford University, http://www.robots.ox.ac.uk/ pnewman

See also

Vehicle, RandomPath, RangeBearingSensor, Map, ParticleFilter

EKF.EKF

EKF object constructor

E = **EKF**(**vehicle**, V_EST, **p0**, **options**) is an **EKF** that estimates the state of the **vehicle** with estimated odometry covariance V_EST (2×2) and initial covariance (3×3).

E = **EKF**(**vehicle**, V_EST, **p0**, **sensor**, W_EST, **map**, **options**) as above but uses information from a **vehicle** mounted sensor, estimated sensor covariance W_EST and a **map**.

Options

'verbose'	Be verbose.
'nohistory'	Don't keep history.
'joseph'	Use Joseph form for covariance.

Notes

- If **map** is [] then it will be estimated.
- If V_EST and **p0** are [] the vehicle is assumed error free and the filter will only estimate the landmark positions (map).
- If V_EST and **p0** are finite the filter will estimate the vehicle pose and the landmark positions (map).
- EKF subclasses Handle, so it is a reference object.

See also

Vehicle, Sensor, RangeBearingSensor, Map

EKF.char

Convert to string

E.**char**() is a string representing the state of the **EKF** object in human-readable form.

See also

EKF.display

EKF.display

Display status of EKF object

E.**display**() displays the state of the **EKF** object in human-readable form.

Notes

- This method is invoked implicitly at the command line when the result of an expression is a EKF object and the command has no trailing semicolon.

See also

EKF.char

EKF.init

Reset the filter

E.**init**() resets the filter state and clears the history.

EKF.plot_ellipse

Plot vehicle covariance as an ellipse

E.plot_ellipse() overlay the current plot with the estimated vehicle position covariance ellipses for 20 points along the path.

E.plot_ellipse(**i**) as above but for **i** points along the path.

E.plot_ellipse(**i**, **ls**) as above but pass line style arguments **ls** to plot_ellipse. If **i** is [] then assume 20.

See also

plot_ellipse

EKF.plot_map

Plot landmarks

E.plot_map(**i**) overlay the current plot with the estimated landmark position (a +-marker) and a covariance ellipses for **i** points along the path.

E.plot_map() as above but **i**=20.

E.plot_map(**i**, **ls**) as above but pass line style arguments **ls** to plot_ellipse.

See also

plot_ellipse

EKF.plot_P

Plot covariance magnitude

E.plot_P() plots the estimated covariance magnitude against time step.

E.plot_P(**ls**) as above but the optional line style arguments **ls** are passed to plot.

m = E.plot_P() returns the estimated covariance magnitude at all time steps as a vector.

EKF.plot_xy

Plot vehicle position

E.plot_xy() overlay the current plot with the estimated vehicle path in the xy-plane.

E.plot_xy(**ls**) as above but the optional line style arguments **ls** are passed to plot.

p = E.plot_xy() returns the estimated vehicle pose trajectory as a matrix ($N \times 3$) where each row is x, y, theta.

See also

EKF.plot_ellipse, EKF.plot_P

EKF.run

Run the filter

E.**run**(**n**) runs the filter for **n** time steps and shows an animation of the vehicle moving.

Notes

- All previously estimated states and estimation history are initially cleared.

---

eul2jac

Euler angle rate Jacobian

J = **eul2jac**(**eul**) is a Jacobian matrix (3×3) that maps Euler angle rates to angular velocity at the operating point **eul**=[PHI, THETA, PSI].

J = **eul2jac**(**phi**, **theta**, **psi**) as above but the Euler angles are passed as separate arguments.

Notes

- Used in the creation of an analytical Jacobian.

See also

rpy2jac, SERIALlINK.JACOBN

---

eul2r

Convert Euler angles to rotation matrix

R = **eul2r**(**phi**, **theta**, **psi**, **options**) is an orthonornal rotation matrix equivalent to the specified Euler angles. These correspond to rotations about the Z, Y, Z axes respectively. If **phi**, **theta**, **psi** are column vectors then they are assumed to represent a trajectory and **R** is a three dimensional matrix, where the last index corresponds to rows of **phi**, **theta**, **psi**.

R = eul2r(**eul**, **options**) as above but the Euler angles are taken from consecutive columns of the passed matrix **eul** = [**phi theta psi**].

Options

'deg' Compute angles in degrees (radians default)

Note

- The vectors **phi**, **theta**, **psi** must be of the same length.

See also

eul2tr, rpy2tr, tr2eul

---

eul2tr

Convert Euler angles to homogeneous transform

T = eul2tr(**phi**, **theta**, **psi**, **options**) is a homogeneous transformation equivalent to the specified Euler angles. These correspond to rotations about the Z, Y, Z axes respectively. If **phi**, **theta**, **psi** are column vectors then they are assumed to represent a trajectory and R is a three dimensional matrix, where the last index corresponds to rows of **phi**, **theta**, **psi**.

T = eul2tr(**eul**, **options**) as above but the Euler angles are taken from consecutive columns of the passed matrix **eul** = [**phi theta psi**].

Options

'deg' Compute angles in degrees (radians default)

Note

- The vectors **phi**, **theta**, **psi** must be of the same length.
- The translational part is zero.

See also

eul2r, rpy2tr, tr2eul

---

gauss2d

Gaussian kernel

out = **gauss2d**(**im**, **sigma**, **C**) is a unit volume Gaussian kernel rendered into matrix **out** ($W \times H$) the same size as **im** ($W \times H$). The Gaussian has a standard deviation of **sigma**. The Gaussian is centered at **C**=[U,V].

---

h2e

Homogeneous to Euclidean

E = **h2e**(**H**) is the Euclidean version (K-1 $\times$ N) of the homogeneous points **H** ($K \times N$) where each column represents one point in P^K.

See also

e2h

---

homline

Homogeneous line from two points

L = **homline**(**x1**, **y1**, **x2**, **y2**) is a vector (3×1) which describes a line in homogeneous form that contains the two Euclidean points (**x1**,**y1**) and (**x2**,**y2**).

Homogeneous points X (3×1) on the line must satisfy **L**'*X = 0.

See also

plot_homline

---

homtrans

Apply a homogeneous transformation

p2 = **homtrans**(**T**, **p**) applies homogeneous transformation **T** to the points stored columnwise in **p**.

- If **T** is in SE(2) (3×3) and
  - **p** is $2 \times N$ (2D points) they are considered Euclidean (R^2)
  - **p** is $3 \times N$ (2D points) they are considered projective ($\mathbf{p}^2$)
- If **T** is in SE(3) (4×4) and
  - **p** is $3 \times N$ (3D points) they are considered Euclidean (R^3)
  - **p** is $4 \times N$ (3D points) they are considered projective ($\mathbf{p}^3$)

tp = **homtrans**(**T**, **T1**) applies homogeneous transformation **T** to the homogeneous transformation **T1**, that is **tp**=**T***T1. If **T1** is a 3-dimensional transformation then **T** is applied to each plane as defined by the first two

dimensions, ie. if **T** = $N \times N$ and **T**=$N \times N \times$ **p** then the result is $N \times N \times$ **p**.

See also

e2h, h2e

---

ishomog

Test if argument is a homogeneous transformation

ishomog(**T**) is true (1) if the argument **T** is of dimension 4×4 or $4 \times 4 \times N$, else false (0).

ishomog(**T**, 'valid') as above, but also checks the validity of the rotation matrix.

See also

isrot, isvec

---

isrot

Test if argument is a rotation matrix

isrot(**R**) is true (1) if the argument is of dimension 3×3 or $3 \times 3 \times N$, else false (0).

isrot(**R**, 'valid') as above, but also checks the validity of the rotation matrix.

See also

ishomog, isvec

---

isvec

Test if argument is a vector

isvec(**v**) is true (1) if the argument **v** is a 3-vector, else false (0).

isvec(**v**, **L**) is true (1) if the argument **v** is a vector of length **L**, either a row- or column-vector. Otherwise false (0).

Notes

- differs from MATLAB builtin function ISVECTOR, the latter returns true for the case of a scalar, **isvec** does not.

See also

ishomog, isrot

---

jtraj

Compute a joint space trajectory between two points

[**q**,**qd**,**qdd**] = **jtraj**(**q0**, **qf**, **m**) is a joint space trajectory **q** (**m** $\times$ N) where the joint coordinates vary from **q0** ($1\times N$) to **qf** ($1\times N$). A quintic (5th order) polynomial is used with default zero boundary conditions for velocity and acceleration. Time is assumed to vary from 0 to 1 in **m** steps. Joint velocity and acceleration can be optionally returned as **qd** (**m** $\times$ N) and **qdd** (**m** $\times$ N) respectively. The trajectory **q**, **qd** and **qdd** are **m** $\times$ N matrices, with one row per time step, and one column per joint.

[**q**,**qd**,**qdd**] = **jtraj**(**q0**, **qf**, **m**, **qd0**, **qdf**) as above but also specifies initial and final joint velocity for the trajectory.

[**q**,**qd**,**qdd**] = **jtraj**(**q0**, **qf**, **T**) as above but the trajectory length is defined by the length of the time vector **T** (**m** $\times$ 1).

[**q**,**qd**,**qdd**] = **jtraj**(**q0**, **qf**, **T**, **qd0**, **qdf**) as above but specifies initial and final joint velocity for the trajectory and a time vector.

See also

ctraj, SerialLink.jtraj

Link

Robot manipulator Link class

A Link object holds all information related to a robot link such as kinematics parameters, rigid-body inertial parameters, motor and transmission parameters.

Methods

A	link transform matrix
RP	joint type: 'R' or 'P'
friction	friction force
nofriction	Link object with friction parameters set to zero
dyn	display link dynamic parameters
islimit	test if joint exceeds soft limit
isrevolute	test if joint is revolute
isprismatic	test if joint is prismatic
display	print the link parameters in human readable form
char	convert to string

Properties (read/write)

theta	kinematic: joint angle
d	kinematic: link offset
a	kinematic: link length
alpha	kinematic: link twist
sigma	kinematic: 0 if revolute, 1 if prismatic
mdh	kinematic: 0 if standard D&H, else 1
offset	kinematic: joint variable offset
qlim	kinematic: joint variable limits [min max]
m	dynamic: link mass
r	dynamic: link COG wrt link coordinate frame 3×1
I	dynamic: link inertia matrix, symmetric 3×3, about link COG.
B	dynamic: link viscous friction (motor referred)
Tc	dynamic: link Coulomb friction
G	actuator: gear ratio
Jm	actuator: motor inertia (motor referred)

Notes

- This is reference class object
- Link objects can be used in vectors and arrays

References

- Robotics, Vision & Control, Chap 7 P. Corke, Springer 2011.

See also

SerialLink, Link.Link

Link.Link

Create robot link object

This is class constructor function which has several call signatures.

L = **Link**() is a **Link** object with default parameters.

L = **Link**(**l1**) is a **Link** object that is a deep copy of the link object **l1**.

L = **Link**(**dh**, **options**) is a link object using the specified kinematic convention and with parameters:

- **dh** = [THETA D A ALPHA SIGMA OFFSET] where OFFSET is a constant displacement between the user joint angle vector and the true kinematic solution.
- **dh** = [THETA D A ALPHA SIGMA] where SIGMA=0 for a revolute and 1 for a prismatic joint, OFFSET is zero.
- **dh** = [THETA D A ALPHA], joint is assumed revolute and OFFSET is zero.

Options

'standard'	for standard D&H parameters (default).
'modified'	for modified D&H parameters.

Examples

A standard Denavit-Hartenberg link

```
L3 = Link([ 0, 0.15005, 0.0203, -pi/2, 0], 'standard');
```

the flag 'standard' is not strictly necessary but adds clarity.

For a modified Denavit-Hartenberg link

```
L3 = Link([ 0, 0.15005, 0.0203, -pi/2, 0], 'modified');
```

Notes

- Link object is a reference object, a subclass of Handle object.
- Link objects can be used in vectors and arrays.
- The parameter D is unused in a revolute joint, it is simply a placeholder in the vector and the value given is ignored.
- The parameter THETA is unused in a prismatic joint, it is simply a placeholder in the vector and the value given is ignored.
- The joint offset is a constant added to the joint angle variable before forward kinematics and subtracted after inverse kinematics. It is useful if you want the robot to adopt a 'sensible' pose for zero joint angle configuration.
- The link dynamic (inertial and motor) parameters are all set to zero. These must be set by explicitly assigning the object properties: m, r, I, Jm, B, Tc, G.

Link.A

Link transform matrix

T = L.A(**q**) is the link homogeneous transformation matrix (4×4) corresponding to the link variable **q** which is either the Denavit-Hartenberg parameter THETA (revolute) or

D (prismatic).

Notes

- For a revolute joint the THETA parameter of the link is ignored, and **q** used instead.
- For a prismatic joint the D parameter of the link is ignored, and **q** used instead.
- The link offset parameter is added to **q** before computation of the transformation matrix.

Link.char

Convert to string

s = L.**char**() is a string showing link parameters in a compact single line format. If L is a vector of **Link** objects return a string with one line per **Link**.

See also

Link.display

Link.display

Display parameters

L.**display**() displays the link parameters in compact single line format. If L is a vector of **Link** objects displays one line per element.

Notes

- This method is invoked implicitly at the command line when the result of an expression is a Link object and the command has no trailing semicolon.

See also

Link.char, Link.dyn, SerialLink.showlink

Link.dyn

Show inertial properties of link

L.**dyn**() displays the inertial properties of the link object in a multi-line format. The properties shown are mass, centre of mass, inertia, friction, gear ratio and motor properties.

If L is a vector of **Link** objects show properties for each link.

See also

SerialLink.dyn

Link.friction

Joint friction force

f = L.**friction**(**qd**) is the joint **friction** force/torque for link velocity **qd**.

Notes

- **friction** values are referred to the motor, not the load.
- Viscous **friction** is scaled up by G^2.
- Coulomb **friction** is scaled up by G.
- The sign of the gear ratio is used to determine the appropriate Coulomb **friction** value in the non-symmetric case.

Link.islimit

Test joint limits

L.**islimit**(**q**) is true (1) if **q** is outside the soft limits set for this joint.

Note

- The limits are not currently used by any Toolbox functions.

Link.isprismatic

Test if joint is prismatic

L.**isprismatic**() is true (1) if joint is prismatic.

See also

Link.isrevolute

Link.isrevolute

Test if joint is revolute

L.**isrevolute**() is true (1) if joint is revolute.

See also

Link.isprismatic

Link.nofriction

Remove friction

ln = L.**nofriction**() is a link object with the same parameters as L except nonlinear (Coulomb) friction parameter is zero.

ln = L.**nofriction**('all') as above except that viscous and Coulomb friction are set to zero.

ln = L.**nofriction**('coulomb') as above except that Coulomb friction is set to zero.

ln = L.**nofriction**('viscous') as above except that viscous friction is set to zero.

Notes

- Forward dynamic simulation can be very slow with finite Coulomb friction.

See also

SerialLink.nofriction, SerialLink.fdyn

Link.RP

Joint type

c = L.**RP**() is a character 'R' or 'P' depending on whether joint is revolute or prismatic respectively. If L is a vector of **Link** objects return a string of characters in joint order.

Link.set.I

Set link inertia

L.I = [Ixx Iyy Izz] set link inertia to a diagonal matrix.

L.I = [Ixx Iyy Izz Ixy Iyz Ixz] set link inertia to a symmetric matrix with specified inertia and product of intertia elements.

L.I = M set **Link** inertia matrix to M (3×3) which must be symmetric.

Link.set.r

Set centre of gravity

L.r = R set the link centre of gravity (COG) to R (3-vector).

Link.set.Tc

Set Coulomb friction

L.Tc = F set Coulomb friction parameters to [F -F], for a symmetric Coulomb friction model.

L.Tc = [FP FM] set Coulomb friction to [FP FM], for an asymmetric Coulomb friction model. FP>0 and FM<0.

See also

Link.friction

---

lspb

Linear segment with parabolic blend

[**s**,**sd**,**sdd**] = **lspb**(**s0**, **sf**, **m**) is a scalar trajectory (**m** $\times$ 1) that varies smoothly from **s0** to **sf** in **m** steps using a constant velocity segment and parabolic blends (a trapezoidal path). Velocity and acceleration can be optionally returned as **sd** (**m** $\times$ 1) and **sdd** (**m** $\times$ 1).

[**s**,**sd**,**sdd**] = **lspb**(**s0**, **sf**, **m**, **v**) as above but specifies the velocity of the linear segment which is normally computed automatically.

[**s**,**sd**,**sdd**] = **lspb**(**s0**, **sf**, **T**) as above but specifies the trajectory in terms of the length of the time vector **T** (**m** $\times$ 1).

[**s**,**sd**,**sdd**] = **lspb**(**s0**, **sf**, **T**, **v**) as above but specifies the velocity of the linear segment which is normally computed automatically and a time vector.

Notes

- If no output arguments are specified **s**, **sd**, and **sdd** are plotted.
- For some values of **v** no solution is possible and an error is flagged.

See also

tpoly, jtraj

Map

Map of planar point features

A Map object represents a square 2D environment with a number of landmark feature points.

Methods

plot	Plot the feature map
feature	Return a specified map feature
display	Display map parameters in human readable form
char	Convert map parameters to human readable string

Properties

map	Matrix of map feature coordinates $2 \times N$
dim	The dimensions of the map region x,y in [-dim,dim]
nfeatures	The number of map features N

Examples

To create a map for an area where X and Y are in the range -10 to +10 metres and with 50 random feature points

```
map = Map(50, 10);
```

which can be displayed by

```
map.plot();
```

Reference

Robotics, Vision & Control, Chap 6, Peter Corke, Springer 2011

See also

RangeBearingSensor, EKF

Map.Map

Map of point feature landmarks

m = **Map**(**n**, **dim**, **options**) is a **Map** object that represents **n** random point features in a planar region bounded by +/-**dim** in the x- and y-directions.

Options

'verbose'	Be verbose

Map.char

Convert vehicle parameters and state to a string

s = M.**char**() is a string showing map parameters in a compact human readable format.

Map.display

Display map parameters

M.**display**() **display** map parameters in a compact human readable form.

Notes

- this method is invoked implicitly at the command line when the result of an expression is a Map object and the command has no trailing semicolon.

See also

map.char

Map.feature

Return the specified map feature

f = M.**feature**(**k**) is the coordinate (2×1) of the **k**'th **feature**.

Map.plot

Plot the map

M.**plot**() plots the feature map in the current figure, as a square region with dimensions given by the M.dim property. Each feature is marked by a black diamond.

M.**plot**(**ls**) plots the feature map as above, but the arguments **ls** are passed to **plot** and override the default marker style.

Notes

- The **plot** is left with HOLD ON.

Map.show

Show the feature map

Notes

- Deprecated, use **plot** method.

Map.verbosity

Set verbosity

M.**verbosity**(**v**) set **verbosity** to **v**, where 0 is silent and greater values display more information.

mdl_Fanuc10L

Create kinematic model of Fanuc AM120iB/10L robot

```
mdl_fanuc10L
```

Script creates the workspace variable R which describes the kinematic characteristics of a Fanuc AM120iB/10L robot using standard DH conventions.

Also defines the workspace vector:

q0 mastering position.

Author

Wynand Swart, Mega Robots CC, P/O Box 8412, Pretoria, 0001, South Africa wynand.swart@gmail.com

See also

SerialLink, mdl_puma560akb, mdl_stanford, mdl_twolink

mdl_MotomanHP6

Create kinematic data of a Motoman HP6 manipulator

```
mdl_motomanHP6
```

Script creates the workspace variable R which describes the kinematic characteristics of a Motoman HP6 manipulator using standard DH conventions.

Also defines the workspace vector:

q0 mastering position.

Author:

Wynand Swart, Mega Robots CC, P/O Box 8412, Pretoria, 0001, South Africa wynand.swart@gmail.com

See also

SerialLink, mdl_puma560akb, mdl_stanford, mdl_twolink

---

mdl_puma560

Create model of Puma 560 manipulator

```
mdl_puma560
```

Script creates the workspace variable p560 which describes the kinematic and dynamic characteristics of a Unimation Puma 560 manipulator using standard DH conventions. The model includes armature inertia and gear ratios.

Also define the workspace vectors:

qz	zero joint angle configuration
qr	vertical 'READY' configuration
qstretch	arm is stretched out in the X direction
qn	arm is at a nominal non-singular configuration

Reference

- "A search for consensus among model parameters reported for the PUMA 560 robot", P. Corke and B. Armstrong-Helouvry, Proc. IEEE Int. Conf. Robotics and Automation, (San Diego), pp. 1608-1613, May 1994.

See also

SerialLink, mdl_puma560akb, mdl_stanford, mdl_twolink

---

mdl_puma560akb

Create model of Puma 560 manipulator

```
mdl_puma560akb
```

Script creates the workspace variable p560m which describes the kinematic and dynamic characterstics of a Unimation Puma 560 manipulator modified DH conventions.

Also defines the workspace vectors:

qz	zero joint angle configuration
qr	vertical 'READY' configuration
qstretch	arm is stretched out in the X direction

References

- "The Explicit Dynamic Model and Inertial Parameters of the Puma 560 Arm" Armstrong, Khatib and Burdick 1986

See also

SerialLink, mdl_puma560, mdl_stanford, mdl_twolink

---

mdl_quadcopter

Dynamic parameters for a quadcopter.

```
mdl_quadcopter
```

Script creates the workspace variable quad which describes the dynamic characterstics of a quadcopter.

Properties

This is a structure with the following elements:

J	Flyer rotational inertia matrix (3×3)
h	Height of rotors above CoG (1×1)
d	Length of flyer arms (1×1)
nb	Number of blades per rotor (1×1)
r	Rotor radius (1×1)
c	Blade chord (1×1)
e	Flapping hinge offset (1×1)
Mb	Rotor blade mass (1×1)
Mc	Estimated hub clamp mass (1×1)
ec	Blade root clamp displacement (1×1)
Ib	Rotor blade rotational inertia (1×1)
Ic	Estimated root clamp inertia (1×1)
mb	Static blade moment (1×1)
Ir	Total rotor inertia (1×1)
Ct	Non-dim. thrust coefficient (1×1)
Cq	Non-dim. torque coefficient (1×1)
sigma	Rotor solidity ratio (1×1)
thetat	Blade tip angle (1×1)
theta0	Blade root angle (1×1)
theta1	Blade twist angle (1×1)
theta75	3/4 blade angle (1×1)
thetai	Blade ideal root approximation (1×1)
a	Lift slope gradient (1×1)
A	Rotor disc area (1×1)
gamma	Lock number (1×1)

References

- Design, Construction and Control of a Large Quadrotor micro air vehicle. P.Pounds, PhD thesis, Australian National University, 2007. http://www.eng.yale.edu/pep5/P_Pounds_Thesis_2008.pdf

See also

sl_quadcopter

---

mdl_S4ABB2p8

Create kinematic model of ABB S4 2.8robot

```
mdl_s4abb2P8
```


Script creates the workspace variable R which describes the kinematic characteristics of an ABB S4 2.8 robot using standard DH conventions.

Also defines the workspace vector:

q0 mastering position.

Author

Wynand Swart, Mega Robots CC, P/O Box 8412, Pretoria, 0001, South Africa wynand.swart@gmail.com

See also

SerialLink, mdl_puma560akb, mdl_stanford, mdl_twolink

---

mdl_stanford

Create model of Stanford arm

```
mdl_stanford
```

Script creates the workspace variable stanf which describes the kinematic and dynamic characteristics of the Stanford (Scheinman) arm.

Also defines the vectors:

qz zero joint angle configuration.

Note

- Gear ratios not currently known, though reflected armature inertia is known, so gear ratios are set to 1.

References

- Kinematic data from ”Modelling, Trajectory calculation and Servoing of a computer controlled arm”. Stanford AIM-177. Figure 2.3
- Dynamic data from “Robot manipulators: mathematics, programming and control” Paul 1981, Tables 6.4, 6.6

See also

SerialLink, mdl_puma560, mdl_puma560akb, mdl_twolink

---

mdl_twolink

Create model of a simple 2-link mechanism

```
mdl_twolink
```

Script creates the workspace variable tl which describes the kinematic and dynamic characteristics of a simple planar 2-link mechanism.

Also defines the vector:

qz corresponds to the zero joint angle configuration.

Notes

- It is a planar mechanism operating in the XY (horizontal) plane and is therefore not affected by gravity.
- Assume unit length links with all mass (unity) concentrated at the joints.

References

- Based on Fig 3-6 (p73) of Spong and Vidyasagar (1st edition).

See also

SerialLink, mdl_puma560, mdl_stanford

---

mstraj

Multi-segment multi-axis trajectory

traj = **mstraj**(**p**, **qdmax**, **q0**, **dt**, **tacc**, **options**) is a multi-segment trajectory ($K \times N$) based on via points **p** ($M \times N$) and axis velocity limits **qdmax** ($1 \times N$). The path comprises linear segments with polynomial blends. The output trajectory matrix has one row per time step, and one column per axis.

- **p** ($M \times N$) is a matrix of via points, 1 row per via point, one column per axis. The last via point is the destination.
- **qdmax** ($1 \times N$) are axis velocity limits which cannot be exceeded, or
- **qdmax** ($M \times 1$) are the durations for each of the M segments
- **q0** ($1 \times N$) are the initial axis coordinates
- **dt** is the time step
- **tacc** (1×1) this acceleration time is applied to all segment transitions
- **tacc** ($1 \times M$) acceleration time for each segment, **tacc**(i) is the acceleration time for the transition from segment i to segment i+1. **tacc**(1) is also the acceleration time at the start of segment 1.

traj = **mstraj**(**segments**, **qdmax**, **q0**, **dt**, **tacc**, **qd0**, **qdf**, **options**) as above but additionally specifies the initial and final axis velocities ($1 \times N$).

Options

'verbose'	Show details.

Notes

- If no output arguments are specified the trajectory is plotted.
- The path length K is a function of the number of via points, **q0**, **dt** and **tacc**.
- The final via point **p**(M,:) is the destination.
- The motion has M segments from **q0** to **p**(1,:) to **p**(2,:) to **p**(M,:).
- All axes reach their via points at the same time.
- Can be used to create joint space trajectories where each axis is a joint coordinate.
- Can be used to create Cartesian trajectories with the "axes" assigned to translation and orientation in RPY or Euler angle form.

See also

mstraj, lspb, ctraj

mtraj

Multi-axis trajectory between two points

[**q**,**qd**,**qdd**] = **mtraj**(**tfunc**, **q0**, **qf**, **m**) is a multi-axis trajectory (**m** $\times$ N) varying from state **q0** ($1 \times N$) to **qf** ($1 \times N$) according to the scalar trajectory function **tfunc** in **m** steps. Joint velocity and acceleration can be optionally returned as **qd** (**m** $\times$ N) and **qdd** (**m** $\times$ N) respectively. The trajectory outputs have one row per time step, and one column per axis.

The shape of the trajectory is given by the scalar trajectory function **tfunc**

```
[S,SD,SDD] = TFUNC(S0, SF, M);
```

and possible values of **tfunc** include @lspb for a trapezoidal trajectory, or @tpoly for a polynomial trajectory.

[**q**,**qd**,**qdd**] = **mtraj**(**tfunc**, **q0**, **qf**, **T**) as above but specifies the trajectory length in terms of the length of the time vector **T** (**m** $\times$ 1).

Notes

- If no output arguments are specified **q**, **qd**, and **qdd** are plotted.
- When **tfunc** is @tpoly the result is functionally equivalent to JTRAJ except that no initial velocities can be specified. JTRAJ is computationally a little more efficient.

See also

jtraj, mstraj, lspb, tpoly

Navigation

Navigation superclass

An abstract superclass for implementing navigation classes.

Methods

plot	Display the occupancy grid
visualize	Display the occupancy grid (deprecated)
plan	Plan a path to goal
path	Return/animate a path from start to goal
display	Display the parameters in human readable form
char	Convert to string
rand	Uniformly distributed random number
randn	Normally distributed random number
randi	Uniformly distributed random integer

Properties (read only)

occgrid	Occupancy grid representing the navigation environment
goal	Goal coordinate
seed0	Random number state

Methods that must be provided in subclass

plan	Generate a plan for motion to goal
next	Returns coordinate of next point along path

Methods that may be overriden in a subclass

goal_set	The goal has been changed by nav.goal = (a,b)
navigate_init	Start of path planning.

Notes

- Subclasses the MATLAB handle class which means that pass by reference semantics apply.
- A grid world is assumed and vehicle position is quantized to grid cells.
- Vehicle orientation is not considered.
- The initial random number state is captured as seed0 to allow rerunning an experiment with an interesting outcome.

See also

Dstar, dxform, PRM, RRT

Navigation.Navigation

Create a Navigation object

n = Navigation(**occgrid**, **options**) is a Navigation object that holds an occupancy grid **occgrid**. A number of options can be be passed.

Options

'navhook', F	Specify a function to be called at every step of path
'goal', G	Specify the goal point (2×1)
'verbose'	Display debugging information
'inflate', K	Inflate all obstacles by K cells.
'private'	Use private random number stream.
'reset'	Reset random number stream.
'seed', S	Set the initial state of the random number stream. S must be a proper random number generator state such as saved in the seed0 property of an earlier run.

Notes

- In the occupancy grid a value of zero means free space and non-zero means occupied (not driveable).
- Obstacle inflation is performed with a round structuring element (kcircle).
- The 'private' option creates a private random number stream for the methods rand, randn and randi. If not given the global stream is used.

Navigation.char

Convert to string

N.**char**() is a string representing the state of the navigation object in human-readable form.

Navigation.display

Display status of navigation object

N.**display**() displays the state of the navigation object in human-readable form.

Notes

- This method is invoked implicitly at the command line when the result of an expression is a Navigation object and the command has no trailing semicolon.

See also

Navigation.char

Navigation.goal_change

Notify change of goal

Invoked when the goal property of the object is changed. Typically this is overriden in a subclass to take particular action such as invalidating a costmap.

Navigation.message

display debug message

N.**message**(**s**) displays the string **s** if the verbose property is true.

N.**message**(**fmt**, **args**) as above but accepts printf() like semantics.

Navigation.navigate_init

Notify start of path

Invoked when the path() method is invoked. Typically overriden in a subclass to take particular action such as computing some path parameters. start is the initial position for this path, and nav.goal is the final position.

Navigation.path

Follow path from start to goal

N.**path**(**start**) animates the robot moving from **start** (2×1) to the goal (which is a property of the object).

N.**path**() as above but first displays the occupancy grid, and prompts the user to click a start location. the object).

x = N.**path**(**start**) returns the **path** ($2 \times M$) from **start** to the goal (which is a property of the object).

The method performs the following steps:

- Get start position interactively if not given
- Initialized navigation, invoke method N.navigate_init()
- Visualize the environment, invoke method N.plot()
- Iterate on the next() method of the subclass

See also

Navigation.plot, Navigation.goal

Navigation.plot

Visualize navigation environment

N.**plot**() displays the occupancy grid in a new figure.

N.**plot**(**p**) as above but overlays the points along the path ($M \times 2$) matrix.

Options

'goal'	Superimpose the goal position if set
'distance', D	Display a distance field D behind the obstacle map. D is a matrix of the same size as the occupancy grid.

Navigation.rand

Uniformly distributed random number

R = N.**rand**() return a uniformly distributed random number from a private random number stream.

R = N.**rand**(**m**) as above but return a matrix (**m** $\times$ **m**) of random numbers.

R = N.**rand**(**L**,**m**) as above but return a matrix (**L** $\times$ **m**) of random numbers.

Notes

- Accepts the same arguments as **rand**().
- Seed is provided to Navigation constructor.

See also

rand, randstream

Navigation.randi

Integer random number

i = N.**randi**(**rm**) return a uniformly distributed random integer in the range 1 to **rm** from a private random number stream.

i = N.**randi**(**rm**, **m**) as above but return a matrix (**m** $\times$ **m**) of random integers.

i = N.**randn**(**rm**, **L**,**m**) as above but return a matrix (**L** $\times$ **m**) of random integers.

Notes

- Accepts the same arguments as **randn**().
- Seed is provided to Navigation constructor.

See also

randn, randstream

Navigation.randn

Normally distributed random number

R = N.**randn**() return a normally distributed random number from a private random number stream.

R = N.**randn**(**m**) as above but return a matrix (**m** $\times$ **m**) of random numbers.

R = N.**randn**(**L**,**m**) as above but return a matrix (**L** $\times$ **m**) of random numbers.

Notes

- Accepts the same arguments as **randn**().
- Seed is provided to Navigation constructor.

See also

randn, randstream

Navigation.spinner

Update progress spinner

N.**spinner**() displays a simple ASCII progress **spinner**, a rotating bar.

Navigation.verbosity

Set verbosity

N.**verbosity**(**v**) set **verbosity** to **v**, where 0 is silent and greater values display more information.

---

numcols

Return number of columns in matrix

nc = **numcols**(**m**) is the number of columns in the matrix **m**.

See also

numrows

---

numrows

Return number of rows in matrix

nr = **numrows**(**m**) is the number of rows in the matrix **m**.

See also

numcols

---

oa2r

Convert orientation and approach vectors to rotation matrix

R = **oa2r**(**o**, **a**) is a rotation matrix for the specified orientation and approach vectors (3×1) formed from 3 vectors such that **R** = [N **o** **a**] and N = **o** x **a**.

Notes

- The submatrix is guaranteed to be orthonormal so long as **o** and **a** are not parallel.
- The vectors **o** and **a** are parallel to the Y- and Z-axes of the coordinate frame.

See also

rpy2r, eul2r, oa2tr

---

oa2tr

Convert orientation and approach vectors to homogeneous transformation

T = **oa2tr**(**o**, **a**) is a homogeneous tranformation for the specified orientation and approach vectors (3×1) formed from 3 vectors such that R = [N **o** **a**] and N = **o** x **a**.

Notes

- The rotation submatrix is guaranteed to be orthonormal so long as **o** and **a** are not parallel.
- The translational part is zero.
- The vectors **o** and **a** are parallel to the Y- and Z-axes of the coordinate frame.

See also

rpy2tr, eul2tr, oa2r

ParticleFilter

Particle filter class

Monte-carlo based localisation for estimating vehicle pose based on odometry and observations of known landmarks.

Methods

run	run the particle filter
plot_xy	display estimated vehicle path
plot_pdf	display particle distribution

Properties

robot	reference to the robot object
sensor	reference to the sensor object
history	vector of structs that hold the detailed information from each time step
nparticles	number of particles used
x	particle states; nparticles x 3
weight	particle weights; nparticles x 1
x_est	mean of the particle population
std	standard deviation of the particle population
Q	covariance of noise added to state at each step
L	covariance of likelihood model
dim	maximum xy dimension

Example

Create a landmark map

```
map = Map(20);
```

and a vehicle with odometry covariance and a driver

```
W = diag([0.1, 1*pi/180].^2);
veh = Vehicle(W);
veh.add_driver( RandomPath(10) );
```

and create a range bearing sensor

```
R = diag([0.005, 0.5*pi/180].^2);
sensor = RangeBearingSensor(veh, map, R);
```

For the particle filter we need to define two covariance matrices. The first is is the covariance of the random noise added to the particle states at each iteration to represent uncertainty in configuration.

```
Q = diag([0.1, 0.1, 1*pi/180]).^2;
```

and the covariance of the likelihood function applied to innovation

```
L = diag([0.1 0.1]);
```

Now construct the particle filter

```
pf = ParticleFilter(veh, sensor, Q, L, 1000);
```

which is configured with 1000 particles. The particles are initially uniformly distributed over the 3-dimensional configuration space.

We run the simulation for 1000 time steps

```
pf.run(1000);
```

then plot the map and the true vehicle path

```
map.plot();
veh.plot_xy('b');
```

and overlay the mean of the particle cloud

```
pf.plot_xy('r');
```

We can plot the standard deviation against time

```
plot(pf.std(1:100,:))
```

The particles are a sampled approximation to the PDF and we can display this as

```
pf.plot_pdf()
```

Acknowledgement

Based on code by Paul Newman, Oxford University, http://www.robots.ox.ac.uk/ pnewman

Reference

Robotics, Vision & Control, Peter Corke, Springer 2011

See also

Vehicle, RandomPath, RangeBearingSensor, Map, EKF

ParticleFilter.ParticleFilter

Particle filter constructor

pf = ParticleFilter(**vehicle**, **sensor**, **q**, **L**, **np**, **options**) is a particle filter that estimates the state of the **vehicle** with a sensor **sensor**. **q** is covariance of the noise added to the particles at each step (diffusion), **L** is the covariance used in the sensor likelihood model, and **np** is the number of particles.

Options

'verbose'	Be verbose.
'private'	Use private random number stream.
'reset'	Reset random number stream.
'seed', S	Set the initial state of the random number stream. S must be a proper random number generator state such as saved in the seed0 property of an earlier run.
'nohistory'	Don't save history.

Notes

- ParticleFilter subclasses Handle, so it is a reference object.
- The initial particle distribution is uniform over the map, essentially the kidnapped robot problem which is quite unrealistic.
- The 'private' option creates a private random number stream for the methods rand, randn and randi. If not given the global stream is used.

See also

Vehicle, Sensor, RangeBearingSensor, Map

ParticleFilter.init

Initialize the particle filter

PF.**init**() initializes the particle distribution and clears the history.

Notes

- Invoked by the run() method.

ParticleFilter.plot_pdf

Plot particles as a PDF

PF.plot_pdf() plots a sparse PDF as a series of vertical line segments of height equal to particle weight.

ParticleFilter.plot_xy

Plot vehicle position

PF.plot_xy() plots the estimated vehicle path in the xy-plane.

PF.plot_xy(**ls**) as above but the optional line style arguments **ls** are passed to plot.

ParticleFilter.run

Run the particle filter

PF.**run**(**n**) runs the filter for **n** time steps.

Notes

- All previously estimated states and estimation history is cleared.

---

peak

Find peaks in vector

yp = **peak**(**y**, **options**) are the values of the maxima in the vector **y**.

[**yp**,**i**] = **peak**(**y**, **options**) as above but also returns the indices of the maxima in the vector **y**.

[**yp**,**xp**] = **peak**(**y**, **x**, **options**) as above but also returns the corresponding x-coordinates of the maxima in the vector **y**. **x** is the same length of **y** and contains the corresponding x-coordinates.

Options

'npeaks', N	Number of peaks to return (default all)
'scale', S	Only consider as peaks the largest value in the horizontal range +/- S points.
'interp', N	Order of interpolation polynomial (default no interpolation)
'plot'	Display the interpolation polynomial overlaid on the point data

Notes

- To find minima, use **peak**(-V).
- The interp options fits points in the neighbourhood about the **peak** with an N'th order polynomial and its **peak** position is returned. Typically choose N to be odd.

See also

peak2

---

peak2

Find peaks in a matrix

zp = **peak2**(**z**, **options**) are the peak values in the 2-dimensional signal **z**.

[**zp**,**ij**] = **peak2**(**z**, **options**) as above but also returns the indices of the maxima in the matrix **z**. Use SUB2IND to convert these to row and column coordinates

Options

'npeaks', N	Number of peaks to return (default all)
'scale', S	Only consider as peaks the largest value in the horizontal and vertical range +/- S points.
'interp'	Interpolate peak (default no interpolation)
'plot'	Display the interpolation polynomial overlaid on the point data

Notes

- To find minima, use **peak2**(-V).
- The interp options fits points in the neighbourhood about the peak with a paraboloid and its peak position is returned.

See also

peak, sub2ind

PGraph

Graph class

g = PGraph()	create a 2D, planar, undirected graph
g = PGraph(n)	create an n-d, undirected graph

Provides support for graphs that:

- are undirected
- are embedded in coordinate system
- have symmetric cost edges (A to B is same cost as B to A)
- have no loops (edges from A to A)
- have vertices are represented by integers vid
- have edges are represented by integers, eid

Methods

Constructing the graph

g.add_node(coord)	add vertex, return vid
g.add_edge(v1, v2)	add edge from v1 to v2, return eid
g.setcost(e, c)	set cost for edge e
g.setdata(v, u)	set user data for vertex v
g.data(v)	get user data for vertex v
g.clear()	remove all vertices and edges from the graph

Information from graph

g.edges(v)	list of edges for vertex v
g.cost(e)	cost of edge e
g.neighbours(v)	neighbours of vertex v
g.component(v)	component id for vertex v
g.connectivity()	number of edges for all vertices

Display

g.plot()	set goal vertex for path planning
g.highlight_node(v)	highlight vertex v
g.highlight_edge(e)	highlight edge e
g.highlight_component(c)	highlight all nodes in component c
g.highlight_path(p)	highlight nodes and edge along path p

g.pick(coord) vertex closest to coord

g.char() convert graph to string
g.display() display summary of graph

Matrix representations

g.adjacency()	adjacency matrix
g.incidence()	incidence matrix
g.degree()	degree matrix
g.laplacian()	Laplacian matrix

Planning paths through the graph

g.Astar(s, g)	shortest path from s to g
g.goal(v)	set goal vertex, and plan paths
g.path(v)	list of vertices from v to goal

Graph and world points

g.coord(v)	coordinate of vertex v
g.distance(v1, v2)	distance between v1 and v2
g.distances(coord)	return sorted distances from coord to all vertices
g.closest(coord)	vertex closest to coord

Object properties (read only)

g.n	number of vertices
g.ne	number of edges
g.nc	number of components

Notes

- Graph connectivity is maintained by a labeling algorithm and this is updated every time an edge is added.
- Nodes and edges cannot be deleted.

PGraph.PGraph

Graph class constructor

g=PGraph(d, options) is a graph object embedded in **d** dimensions.

Options

'distance', M	Use the distance metric M for path planning which is either 'Euclidean' (default) or 'SE2'.
'verbose'	Specify verbose operation

Note

- Number of dimensions is not limited to 2 or 3.
- The distance metric 'SE2' is the sum of the squares of the difference in position and angle modulo 2pi.
- To use a different distance metric create a subclass of PGraph and override the method distance_metric().

PGraph.add_edge

Add an edge

E = G.add_edge(**v1**, **v2**) adds an edge between vertices with id **v1** and **v2**, and returns the edge id **E**. The edge cost is the distance between the vertices.

E = G.add_edge(**v1**, **v2**, **C**) as above but the edge cost is **C**. cost **C**.

Note

- Graph connectivity is maintained by a labeling algorithm and this is updated every time an edge is added.

See also

PGraph.add_node

PGraph.add_node

Add a node

v = G.add_node(**x**) adds a node/vertex with coordinate **x** ($D \times 1$) and returns the integer node id **v**.

v = G.add_node(**x**, **v2**) as above but connected by an edge to vertex **v2** with cost equal to the distance between the vertices.

v = G.add_node(**x**, **v2**, **C**) as above but the added edge has cost **C**.

See also

PGraph.add_edge, PGraph.data, PGraph.getdata

PGraph.adjacency

Adjacency matrix of graph

a = G.**adjacency**() is a matrix ($N \times N$) where element **a**(i,j) is the cost of moving from vertex i to vertex j.

Notes

- Matrix is symmetric.
- Eigenvalues of **a** are real and are known as the spectrum of the graph.
- The element **a**(I,J) can be considered the number of walks of one edge from vertex I to vertex J (either zero or one). The element (I,J) of $\mathbf{a}^N$ are the number of walks of length N from vertex I to vertex J.

See also

PGraph.degree, PGraph.incidence, PGraph.laplacian

PGraph.Astar

path finding

path = G.**Astar**(**v1**, **v2**) is the lowest cost path from vertex **v1** to vertex **v2**. **path** is a list of vertices starting with **v1** and ending **v2**.

[**path**,**C**] = G.**Astar**(**v1**, **v2**) as above but also returns the total cost of traversing **path**.

Notes

- Uses the efficient A* search algorithm.

References

- Correction to "A Formal Basis for the Heuristic Determination of Minimum Cost Paths". Hart, P. E.; Nilsson, N. J.; Raphael, B. SIGART Newsletter 37: 28-29, 1972.

See also

PGraph.goal, PGraph.path

PGraph.char

Convert graph to string

s = G.**char**() is a compact human readable representation of the state of the graph including the number of vertices, edges and components.

PGraph.clear

Clear the graph

G.**clear**() removes all vertices, edges and components.

PGraph.closest

Find closest vertex

v = G.**closest**(**x**) is the vertex geometrically **closest** to coordinate **x**.

[**v**,**d**] = G.**closest**(**x**) as above but also returns the distance **d**.

See also

PGraph.distances

PGraph.component

Graph component

C = G.**component**(**v**) is the id of the graph **component**

PGraph.connectivity

Graph connectivity

C = G.**connectivity**() is a vector ($N \times 1$) with the number of edges per vertex.

The average vertex **connectivity** is

```
mean(g.connectivity())
```

and the minimum vertex **connectivity** is

```
min(g.connectivity())
```


PGraph.coord

Coordinate of node

x = G.**coord**(**v**) is the coordinate vector ($D \times 1$) of vertex id **v**.

PGraph.cost

Cost of edge

C = G.**cost**(**E**) is the **cost** of edge id **E**.

PGraph.data

Get user data for node

u = G.**data**(**v**) gets the user **data** of vertex **v** which can be of any type such as number, struct, object or cell array.

See also

PGraph.setdata

PGraph.degree

Degree matrix of graph

d = G.**degree**() is a diagonal matrix ($N \times N$) where element **d**(i,i) is the number of edges connected to vertex id i.

See also

PGraph.adjacency, PGraph.incidence, PGraph.laplacian

PGraph.display

Display graph

G.**display**() displays a compact human readable representation of the state of the graph including the number of vertices, edges and components.

See also

PGraph.char

PGraph.distance

Distance between vertices

d = G.**distance**(**v1**, **v2**) is the geometric **distance** between the vertices **v1** and **v2**.

See also

PGraph.distances

PGraph.distances

Distances from point to vertices

d = G.**distances**(**x**) is a vector $(1 \times N)$ of geometric distance from the point **x** (**d** $\times$ 1) to every other vertex sorted into increasing order.

[**d**,**w**] = G.**distances**(**p**) as above but also returns **w** $(1 \times N)$ with the corresponding vertex id.

See also

PGraph.closest

PGraph.edges

Find edges given vertex

E = G.**edges**(**v**) return the id of all **edges** from vertex id **v**.

PGraph.get.n

Number of vertices

G.n is the number of vertices in the graph.

See also

PGraph.ne

PGraph.get.nc

Number of components

G.nc is the number of components in the graph.

See also

PGraph.component

PGraph.get.ne

Number of edges

G.ne is the number of **edges** in the graph.

See also

PGraph.n

PGraph.goal

Set goal node

G.goal(**vg**) computes the cost of reaching every vertex in the graph connected to the goal vertex **vg**.

Notes

- Combined with G.path performs a breadth-first search for paths to the goal.

See also

PGraph.path, PGraph.Astar

PGraph.highlight_component

Highlight a graph component

G.highlight_component(**C**, **options**) highlights the vertices that belong to graph component **C**.

Options

'NodeSize', S	Size of vertex circle (default 12)
'NodeFaceColor', **C**	Node circle color (default yellow)
'NodeEdgeColor', **C**	Node circle edge color (default blue)

See also

PGraph.highlight_node, PGraph.highlight_edge, PGraph.highlight_component

PGraph.highlight_edge

Highlight a node

G.highlight_edge(**v1**, **v2**) highlights the edge between vertices **v1** and **v2**.

G.highlight_edge(**E**) highlights the edge with id **E**.

Options

'EdgeColor', C	Edge edge color (default black)
'EdgeThickness', T	Edge thickness (default 1.5)

See also

PGraph.highlight_node, PGraph.highlight_path, PGraph.highlight_component

---

PGraph.highlight_node

Highlight a node

G.highlight_node(**v**, **options**) highlights the vertex **v** with a yellow marker. If **v** is a list of vertices then all are highlighted.

Options

'NodeSize', S	Size of vertex circle (default 12)
'NodeFaceColor', C	Node circle color (default yellow)
'NodeEdgeColor', C	Node circle edge color (default blue)

See also

PGraph.highlight_edge, PGraph.highlight_path, PGraph.highlight_component

---

PGraph.highlight_path

Highlight path

G.highlight_path(**p**, **options**) highlights the path defined by vector **p** which is a list of vertices comprising the path.

Options

'NodeSize', S	Size of vertex circle (default 12)
'NodeFaceColor', C	Node circle color (default yellow)
'NodeEdgeColor', C	Node circle edge color (default blue)
'EdgeColor', C	Node circle edge color (default black)

See also

PGraph.highlight_node, PGraph.highlight_edge, PGraph.highlight_component

---

PGraph.incidence

Incidence matrix of graph

in = G.**incidence**() is a matrix ($N \times NE$) where element **in**(i,j) is non-zero if vertex id i is connected to edge id j.

See also

PGraph.adjacency, PGraph.degree, PGraph.laplacian

PGraph.laplacian

Laplacian matrix of graph

L = G.**laplacian**() is the Laplacian matrix ($N \times N$) of the graph.

Notes

- **L** is always positive-semidefinite.
- **L** has at least one zero eigenvalue.
- The number of zero eigenvalues is the number of connected components in the graph.

See also

PGraph.adjacency, PGraph.incidence, PGraph.degree

PGraph.merge

the dominant and submissive labels

PGraph.neighbours

Neighbours of a vertex

n = G.**neighbours**(**v**) is a vector of ids for all vertices which are directly connected **neighbours** of vertex **v**.

[**n**,**C**] = G.**neighbours**(**v**) as above but also returns a vector **C** whose elements are the edge costs of the paths corresponding to the vertex ids in **n**.

PGraph.path

Find path to goal node

p = G.**path**(**vs**) is a vector of vertex ids that form a **path** from the starting vertex **vs** to the previously specified goal. The **path** includes the start and goal vertex id.

To compute **path** to goal vertex 5

```
g.goal(5);
```

then the **path**, starting from vertex 1 is

```
p1 = g.path(1);
```

and the **path** starting from vertex 2 is

```
p2 = g.path(2);
```

Notes

- Pgraph.goal must have been invoked first.
- Can be used repeatedly to find paths from different starting points to the goal specified to Pgraph.goal().

See also

PGraph.goal, PGraph.Astar

PGraph.pick

Graphically select a vertex

v = G.**pick**() is the id of the vertex closest to the point clicked by the user on a plot of the graph.

See also

PGraph.plot

PGraph.plot

Plot the graph

G.**plot**(**opt**) plots the graph in the current figure. Nodes are shown as colored circles.

Options

'labels'	Display vertex id (default false)
'edges'	Display edges (default true)
'edgelabels'	Display edge id (default false)
'NodeSize', S	Size of vertex circle (default 8)
'NodeFaceColor', C	Node circle color (default blue)
'NodeEdgeColor', C	Node circle edge color (default blue)
'NodeLabelSize', S	Node label text sizer (default 16)
'NodeLabelColor', C	Node label text color (default blue)
'EdgeColor', C	Edge color (default black)
'EdgeLabelSize', S	Edge label text size (default black)
'EdgeLabelColor', C	Edge label text color (default black)
'componentcolor'	Node color is a function of graph component

PGraph.setcost

Set cost of edge

G.**setcost**(**E**, **C**) set cost of edge id **E** to **C**.

PGraph.setdata

Set user data for node

G.**setdata**(**v**, **u**) sets the user data of vertex **v** to **u** which can be of any type such as number, struct, object or cell array.

See also

PGraph.data

PGraph.vertices

Find vertices given edge

v = G.**vertices**(**E**) return the id of the **vertices** that define edge **E**.

---

plot2

Plot trajectories

plot2(**p**) plots a line with coordinates taken from successive rows of **p**. **p** can be $N \times 2$ or $N \times 3$.

If **p** has three dimensions, ie. $N \times 2 \times M$ or $N \times 3 \times M$ then the M trajectories are overlaid in the one plot.

plot2(**p**, **ls**) as above but the line style arguments **ls** are passed to plot.

See also

plot

---

plot_arrow

Plot arrow

PLOT_ARROW(**p**, **options**) draws an arrow from P1 to P2 where **p**=[P1; P2].

See also

arrow3

---

plot_box

a box on the current plot

PLOT_BOX(**b**, **ls**) draws a box defined by **b**=[XL XR; YL YR] with optional Matlab linestyle options **ls**.

PLOT_BOX(**x1**,**y1**, **x2**,**y2**, **ls**) draws a box with corners at (**x1**,**y1**) and (**x2**,**y2**), and optional Matlab linestyle options **ls**.

PLOT_BOX('centre', P, 'size', W, **ls**) draws a box with center at P=[X,Y] and with dimensions W=[WIDTH HEIGHT].

PLOT_BOX('topleft', P, 'size', W, **ls**) draws a box with top-left at P=[X,Y] and with dimensions W=[WIDTH HEIGHT].

---

plot_circle

Draw a circle on the current plot

PLOT_CIRCLE(**C**, **R**, **options**) draws a circle on the current plot with centre **C**=[X,Y] and radius **R**. If **C**=[X,Y,Z] the circle is drawn in the XY-plane at height Z.

Options

'edgecolor'	the color of the circle's edge, Matlab color spec
'fillcolor'	the color of the circle's interior, Matlab color spec
'alpha'	transparency of the filled circle: 0=transparent, 1=solid.

---

plot_ellipse

Draw an ellipse on the current plot

PLOT_ELLIPSE(**a**, **ls**) draws an ellipse defined by X'AX = 0 on the current plot, centred at the origin, with Matlab line style **ls**.

PLOT_ELLIPSE(**a**, **C**, **ls**) as above but centred at **C**=[X,Y]. current plot. If **C**=[X,Y,Z] the ellipse is parallel to the XY plane but at height Z.

See also

plot_circle

---

plot_homline

Draw a line in homogeneous form

H = PLOT_HOMLINE(**L**, **ls**) draws a line in the current figure **L**.X = 0. The current axis limits are used to determine the endpoints of the line. Matlab line specification **ls** can be set.

The return argument is a vector of graphics handles for the lines.

See also

homline

---

plot_point

point features

PLOT_POINT(**p**, **options**) adds point markers to a plot, where **p** ($2 \times N$) and each column is the point coordinate.

Options

'textcolor', colspec	Specify color of text
'textsize', size	Specify size of text
'bold'	Text in bold font.
'printf', fmt, data	Label points according to printf format string and corresponding element of data
'sequence'	Label points sequentially

Additional options are passed through to PLOT for creating the marker.

Examples

Simple point plot


```
P = rand(2,4);
plot_point(P);
```

Plot points with markers

```
plot_point(P, '*');
```

Plot points with square markers and labels

```
plot_point(P, 'sequence', 's');
```

Plot points with circles and annotations

```
data = [1 2 4 8];
plot_point(P, 'printf', {' P%d', data}, 'o');
```

See also

plot, text

---

plot_poly

Plot a polygon

plotpoly(**p**, **options**) plot a polygon defined by columns of **p** which can be $2 \times N$ or $3 \times N$.

options

'fill'	the color of the circle's interior, Matlab color spec
'alpha'	transparency of the filled circle: 0=transparent, 1=solid.

See also

plot, patch, Polygon

---

plot_sphere

Plot spheres

PLOT_SPHERE(**C**, **R**, **color**) add spheres to the current figure. **C** is the centre of the sphere and if its a $3 \times N$ matrix then N spheres are drawn with centres as per the

columns. **R** is the radius and **color** is a Matlab color spec, either a letter or 3-vector.

H = PLOT_SPHERE(**C**, **R**, **color**) as above but returns the handle(s) for the spheres.

H = PLOT_SPHERE(**C**, **R**, **color**, **alpha**) as above but **alpha** specifies the opacity of the sphere were 0 is transparant and 1 is opaque. The default is 1.

NOTES

- The sphere is always added, irrespective of figure hold state.
- The number of vertices to draw the sphere is hardwired.

---

plot_vehicle

Plot ground vehicle pose

plot_vehicle(**x**,**options**) draw representation of ground robot as an oriented triangle with pose **x** (1×3) [x,y,theta] or **x** (3×3) as homogeneous transform in SE(2).

Options

'scale', S	Draw vehicle with length S x maximum axis dimension
'size', S	Draw vehicle with length S

See also

Vehicle.plot

---

plotbotopt

Define default options for robot plotting

A user provided function that returns a cell array of default plot options for the SerialLink.plot method.

See also

SerialLink.plot

---

plotp

Plot trajectories

plotp(**p**) plots a set of points **p**, which by Toolbox convention are stored one per column. **p** can be $N \times 2$ or $N \times 3$. By default a linestyle of 'bx' is used.

plotp(**p**, **ls**) as above but the line style arguments **ls** are passed to plot.

See also

plot, plot2

---

polydiff

pd = polydiff(p)

Return the coefficients of the derivative of polynomial p

Polygon

Polygon class

A general class for manipulating polygons and vectors of polygons.

Methods

plot	Plot polygon
area	Area of polygon
moments	Moments of polygon
centroid	Centroid of polygon
perimeter	Perimter of polygon
transform	Transform polygon
inside	Test if points are inside polygon
intersection	Intersection of two polygons
difference	Difference of two polygons
union	Union of two polygons
xor	Exclusive or of two polygons
display	print the polygon in human readable form
char	convert the polgyon to human readable string

Properties

vertices	List of polygon vertices, one per column
extent	Bounding box [minx maxx; miny maxy]
n	Number of vertices

Notes

- This is reference class object
- Polygon objects can be used in vectors and arrays

Acknowledgement

The methods inside, intersection, difference, union, and xor are based on code written by:

Kirill K. Pankratov, kirill@plume.mit.edu, http://puddle.mit.edu/ glenn/kirill/saga.html

and require a licence. However the author does not respond to email regarding the licence, so use with care, and modify with acknowledgement.

Polygon.Polygon

Polygon class constructor

p = **Polygon**(**v**) is a polygon with vertices given by **v**, one column per vertex.

p = **Polygon**(**C**, **wh**) is a rectangle centred at **C** with dimensions **wh**=[WIDTH, HEIGHT].

Polygon.area

Area of polygon

a = P.**area**() is the **area** of the polygon.

Polygon.centroid

Centroid of polygon

x = P.**centroid**() is the **centroid** of the polygon.

Polygon.char

String representation

s = P.**char**() is a compact representation of the polgyon in human readable form.

Polygon.difference

Difference of polygons

d = P.**difference**(**q**) is polygon P minus polygon **q**.

Notes

- If polygons P and **q** are not intersecting, returns coordinates of P.
- If the result **d** is not simply connected or consists of several polygons, resulting vertex list will contain NaNs.

Polygon.display

Display polygon

P.**display**() displays the polygon in a compact human readable form.

See also

Polygon.char

Polygon.inside

Test if points are inside polygon

in = **p**.**inside**(**p**) tests if points given by columns of **p** are **inside** the polygon. The corresponding elements of **in** are either true or false.

Polygon.intersect

Intersection of polygon with list of polygons

i = P.**intersect**(**plist**) indicates whether or not the **Polygon** P intersects with

i(**j**) = 1 if p intersects polylist(**j**), else 0.

Polygon.intersect_line

Intersection of polygon and line segment

i = P.intersect_line(**L**) is the intersection points of a polygon P with the line segment **L**=[x1 x2; y1 y2]. **i** is an $N \times 2$ matrix with one column per intersection, each column is [x y]'.

Polygon.intersection

Intersection of polygons

i = P.**intersection**(**q**) is a **Polygon** representing the **intersection** of polygons P and **q**.

Notes

- If these polygons are not intersecting, returns empty polygon.
- If **intersection** consist of several disjoint polygons (for non-convex P or **q**) then vertices of **i** is the concatenation of the vertices of these polygons.

Polygon.moments

Moments of polygon

a = P.**moments**(**p**, **q**) is the pq'th moment of the polygon.

See also

mpq_poly

Polygon.perimeter

Perimeter of polygon

L = P.**perimeter**() is the **perimeter** of the polygon.

Polygon.plot

Plot polygon

P.**plot**() **plot** the polygon.

P.**plot**(**ls**) as above but pass the arguments **ls** to **plot**.

Polygon.transform

Transformation of polygon vertices

p2 = P.**transform**(**T**) is a new **Polygon** object whose vertices have been transfored by the 3×3 homgoeneous transformation **T**.

Polygon.union

Union of polygons

i = P.**union**(**q**) is a **Polygon** representing the **union** of polygons P and **q**.

Notes

- If these polygons are not intersecting, returns a polygon with vertices of both polygons separated by NaNs.
- If the result P is not simply connected (such as a polygon with a "hole") the resulting contour consist of counter- clockwise "outer boundary" and one or more clock-wise "inner boundaries" around "holes".

Polygon.xor

Exclusive or of polygons

i = P.**union**(**q**) is a **Polygon** representing the **union** of polygons P and **q**.

Notes

- If these polygons are not intersecting, returns a polygon with vertices of both polygons separated by NaNs.
- If the result P is not simply connected (such as a polygon with a "hole") the resulting contour consist of counter- clockwise "outer boundary" and one or more clock-wise "inner boundaries" around "holes".

PRM

Probabilistic RoadMap navigation class

A concrete subclass of the Navigation class that implements the probabilistic roadmap navigation algorithm. This performs goal independent planning of roadmaps, and at the query stage finds paths between specific start and goal points.

Methods

plan	Compute the roadmap
path	Compute a path to the goal
visualize	Display the obstacle map (deprecated)
plot	Display the obstacle map
display	Display the parameters in human readable form
char	Convert to string

Example

```
load map1               % load map
goal = [50,30];         % goal point
start = [20, 10];       % start point
prm = PRM(map);         % create navigation object
prm.plan()              % create roadmaps
prm.path(start, goal)   % animate path from this start location
```

References

- Probabilistic roadmaps for path planning in high dimensional configuration spaces, L. Kavraki, P. Svestka, J. Latombe, and M. Overmars, IEEE Transactions on Robotics and Automation, vol. 12, pp. 566-580, Aug 1996.
- Robotics, Vision & Control, Section 5.2.4, P. Corke, Springer 2011.

See also

Navigation, DXform, Dstar, PGraph

PRM.PRM

Create a PRM navigation object

p = **PRM**(**map**, **options**) is a probabilistic roadmap navigation object, and **map** is an occupancy grid, a representation of a planar world as a matrix whose elements are 0 (free space) or 1 (occupied).

Options

'npoints', N	Number of sample points (default 100)
'distthresh', D	Distance threshold, edges only connect vertices closer than D (default 0.3 max(size(occgrid)))

Other **options** are supported by the Navigation superclass.

See also

Navigation.Navigation

PRM.char

Convert to string

P.**char**() is a string representing the state of the **PRM** object in human-readable form.

See also

PRM.display

PRM.path

Find a path between two points

P.**path**(**start**, **goal**) finds and displays a **path** from **start** to **goal** which is overlaid on the occupancy grid.

x = P.**path**(**start**) returns the **path** ($2 \times M$) from **start** to **goal**.

PRM.plan

Create a probabilistic roadmap

P.**plan**() creates the probabilistic roadmap by randomly sampling the free space in the map and building a graph with edges connecting close points. The resulting graph is kept within the object.

PRM.plot

Visualize navigation environment

P.**plot**() displays the occupancy grid with an optional distance field.

Options

'goal'	Superimpose the goal position if set
'nooverlay'	Don't overlay the PRM graph

qplot

plot joint angles

qplot(**q**) is a convenience function to plot joint angle trajectories ($M \times 6$) for a 6-axis robot, where each row represents one time step.

The first three joints are shown as solid lines, the last three joints (wrist) are shown as dashed lines. A legend is also displayed.

qplot(**T**, **q**) as above but displays the joint angle trajectory versus time **T** ($M \times 1$).

See also

jtraj, plot

Quaternion

Quaternion class

A quaternion is a compact method of representing a 3D rotation that has computational advantages including speed and numerical robustness. A quaternion has 2 parts, a scalar s, and a vector v and is typically written: q = s <vx, vy, vz>.

A unit-quaternion is one for which $s^2+vx^2+vy^2+vz^2 = 1$. It can be considered as a rotation by an angle theta about a unit-vector V in space where

```
q = cos (theta/2) < v sin(theta/2)>
```

q = **quaternion**(**x**) is a unit-**quaternion** equivalent to **x** which can be any of:

- orthonormal rotation matrix.
- homogeneous transformation matrix (rotation part only).
- rotation angle and vector

Methods

inv	inverse of quaterion
norm	norm of **quaternion**
unit	unitized **quaternion**
plot	same options as trplot()
interp	interpolation (slerp) between q and q2, 0<=s<=1
scale	interpolation (slerp) between identity and q, 0<=s<=1
dot	derivative of **quaternion** with angular velocity w
R	equivalent 3×3 rotation matrix
T	equivalent 4×4 homogeneous transform matrix

Arithmetic operators are overloaded

q1==q2	test for **quaternion** equality
q1 =q2	test for **quaternion** inequality
q+q2	elementwise sum of quaternions
q-q2	elementwise difference of quaternions
q*q2	**quaternion** product
q*v	rotate vector by **quaternion**, v is 3×1
s*q	elementwise multiplication of **quaternion** by scalar
q/q2	q*q2.inv
q^n	q to power n (integer only)

Properties (read only)

s	real part
v	vector part

Notes

- **quaternion** objects can be used in vectors and arrays

References

- Animating rotation with **quaternion** curves, K. Shoemake, in Proceedings of ACM SIGGRAPH, (San Fran cisco), pp. 245-254, 1985.
- On homogeneous transforms, quaternions, and computational efficiency, J. Funda, R. Taylor, and R. Paul, IEEE Transactions on Robotics and Automation, vol. 6, pp. 382-388, June 1990.
- Robotics, Vision & Control, P. Corke, Springer 2011.

See also

trinterp, trplot

Quaternion.Quaternion

Constructor for quaternion objects

Construct a **quaternion** from various other orientation representations.

q = **Quaternion**() is the identitity quaternion 1<0,0,0> representing a null rotation.

q = **Quaternion**(**q1**) is a copy of the quaternion **q1**

q = **Quaternion**([S V1 V2 V3]) is a quaternion formed by specifying directly its 4 elements

q = **Quaternion**(**s**) is a quaternion formed from the scalar **s** and zero vector part: **s**<0,0,0>

q = **Quaternion**(**v**) is a pure quaternion with the specified vector part: 0<**v**>

q = **Quaternion**(**th**, **v**) is a unit-quaternion corresponding to rotation of **th** about the vector **v**.

q = **Quaternion**(**R**) is a unit-quaternion corresponding to the orthonormal rotation matrix **R**. If **R** $(3 \times 3 \times N)$ is a sequence then **q** $(N \times 1)$ is a vector of Quaternions corresponding to the elements of **R**.

q = **Quaternion**(**T**) is a unit-quaternion equivalent to the rotational part of the homogeneous transform **T**. If **T** $(4 \times 4 \times N)$ is a sequence then **q** $(N \times 1)$ is a vector of Quaternions corresponding to the elements of **T**.

Quaternion.char

Convert to string

s = Q.**char**() is a compact string representation of the quaternion's value as a 4-tuple. If Q is a vector then **s** has one line per element.

Quaternion.display

Display the value of a quaternion object

Q.**display**() displays a compact string representation of the quaternion's value as a 4-tuple. If Q is a vector then S has one line per element.

Notes

- This method is invoked implicitly at the command line when the result of an expression is a Quaternion object and the command has no trailing semicolon.

See also

Quaternion.char

Quaternion.double

Convert a quaternion to a 4-element vector

v = Q.**double**() is a 4-vector comprising the quaternion elements [s vx vy vz].

Quaternion.eq

Test quaternion equality

Q1==Q2 is true if the quaternions Q1 and Q2 are equal.

Notes

- Overloaded operator '=='.
- Note that for unit Quaternions Q and -Q are the equivalent rotation, so non-equality does not mean rotations are not equivalent.
- If Q1 is a vector of quaternions, each element is compared to Q2 and the result is a logical array of the same length as Q1.
- If Q2 is a vector of quaternions, each element is compared to Q1 and the result is a logical array of the same length as Q2.
- If Q1 and Q2 are vectors of the same length, then the result is a logical array

See also

Quaternion.ne

Quaternion.interp

Interpolate quaternions

qi = Q1.**interp**(**q2**, **s**) is a unit-quaternion that interpolates a rotation between Q1 for **s**=0 and **q2** for **s**=1.

If **s** is a vector **qi** is a vector of quaternions, each element corresponding to sequential elements of **s**.

Notes

- This is a spherical linear interpolation (slerp) that can be interpretted as interpolation along a great circle arc on a sphere.
- The value of **s** is clipped to the interval 0 to 1.

See also

ctraj, Quaternion.scale

Quaternion.inv

Invert a unit-quaternion

qi = Q.**inv**() is a quaternion object representing the inverse of Q.

Quaternion.minus

Subtract quaternions

Q1-Q2 is the element-wise difference of quaternion elements.

Notes

- Overloaded operator '-'
- The result is not guaranteed to be a unit-quaternion.

See also

Quaternion.plus, Quaternion.mtimes

Quaternion.mpower

Raise quaternion to integer power

Q^N is the quaternion Q raised to the integer power N.

Notes

- Overloaded operator '^'
- Computed by repeated multiplication.

See also

Quaternion.mrdivide, Quaternion.mpower, Quaternion.plus, Quaternion.minus

Quaternion.mrdivide

Quaternion quotient.

Q1/Q2	is a quaternion formed by Hamilton product of Q1 and **inv**(Q2).
Q/S	is the element-wise division of quaternion elements by the scalar S.

Notes

- Overloaded operator '/'

See also

Quaternion.mtimes, Quaternion.mpower, Quaternion.plus, Quaternion.minus

Quaternion.mtimes

Multiply a quaternion object

Q1*Q2	is a quaternion formed by the Hamilton product of two quaternions.
Q*V	is a vector formed by rotating the vector V by the quaternion Q.
Q*S	is the element-wise multiplication of quaternion elements by the scalar S.

Notes

- Overloaded operator '*'

See also

Quaternion.mrdivide, Quaternion.mpower, Quaternion.plus, Quaternion.minus

Quaternion.ne

Test quaternion inequality

Q1 =Q2 is true if the quaternions Q1 and Q2 are not equal.

Notes

- Overloaded operator ' ='
- Note that for unit Quaternions Q and -Q are the equivalent rotation, so non-equality does not mean rotations are not equivalent.
- If Q1 is a vector of quaternions, each element is compared to Q2 and the result is a logical array of the same length as Q1.
- If Q2 is a vector of quaternions, each element is compared to Q1 and the result is a logical array of the same length as Q2.
- If Q1 and Q2 are vectors of the same length, then the result is a logical array.

See also

Quaternion.eq

Quaternion.norm

Quaternion magnitude

qn = q.norm(q) is the scalar **norm** or magnitude of the quaternion **q**.

Notes

- This is the Euclidean **norm** of the quaternion written as a 4-vector.
- A unit-quaternion has a **norm** of one.

See also

Quaternion.unit

Quaternion.plot

Plot a quaternion object

Q.**plot**(**options**) plots the quaternion as a rotated coordinate frame.

Options

Options are passed to trplot and include:

'color', C	The color to draw the axes, MATLAB colorspec C
'frame', F	The frame is named F and the subscript on the axis labels is F.
'view', V	Set **plot** view parameters V=[az el] angles, or 'auto' for view toward origin of coordinate frame

See also

trplot

Quaternion.plus

Add quaternions

Q1+Q2 is the element-wise sum of quaternion elements.

Notes

- Overloaded operator '+'
- The result is not guaranteed to be a unit-quaternion.

See also

Quaternion.minus, Quaternion.mtimes

Quaternion.R

Convert toorthonormal rotation matrix

R = Q.**R**() is the equivalent 3×3 orthonormal rotation matrix.

Notes:

- For a quaternion sequence returns a rotation matrix sequence.

Quaternion.scale

Interpolate rotations expressed by quaternion objects

qi = Q.**scale**(**s**) is a unit-quaternion that interpolates between identity for **s**=0 to Q for **s**=1. This is a spherical linear interpolation (slerp) that can be interpretted as interpolation along a great circle arc on a sphere.

If **s** is a vector **qi** is a cell array of quaternions, each element corresponding to sequential elements of **s**.

Notes

- This is a spherical linear interpolation (slerp) that can be interpretted as interpolation along a great circle arc on a sphere.

See also

ctraj, Quaternion.interp

Quaternion.T

Convert to homogeneous transformation matrix

T = Q.**T**() is the equivalent 4×4 homogeneous transformation matrix.

Notes:

- For a quaternion sequence returns a homogeneous transform matrix sequence
- Has a zero translational component.

Quaternion.unit

Unitize a quaternion

qu = Q.**unit**() is a **unit**-quaternion representing the same orientation as Q.

See also

Quaternion.norm

---

r2t

Convert rotation matrix to a homogeneous transform

T = **r2t**(**R**) is a homogeneous transform equivalent to an orthonormal rotation matrix **R** with a zero translational component.

Notes

- Works for **T** in either SE(2) or SE(3)
  - if **R** is 2×2 then **T** is 3×3, or
  - if **R** is 3×3 then **T** is 4×4.
- Translational component is zero.
- For a rotation matrix sequence returns a homogeneous transform sequence.

See also

t2r

---

randinit

Reset random number generator

RANDINIT reset the defaul random number stream.

See also

randstream

RandomPath

Vehicle driver class

Create a "driver" object capable of driving a Vehicle object through random waypoints within a rectangular region and at constant speed.

The driver object is attached to a Vehicle object by the latter's add_driver() method.

Methods

init	reset the random number generator
demand	return speed and steer angle to next waypoint
display	display the state and parameters in human readable form
char	convert to string

Properties

goal	current goal coordinate
veh	the Vehicle object being controlled
dim	dimensions of the work space (2×1) [m]
speed	speed of travel [m/s]
closeenough	proximity to waypoint at which next is chosen [m]

Example

```
veh = Vehicle(V);
veh.add_driver( RandomPath(20, 2) );
```

Notes

- It is possible in some cases for the vehicle to move outside the desired region, for instance if moving to a waypoint near the edge, the limited turning circle may cause the vehicle to temporarily move outside.
- The vehicle chooses a new waypoint when it is closer than property closeenough to the current waypoint.
- Uses its own random number stream so as to not influence the performance of other randomized algorithms such as path planning.

Reference

Robotics, Vision & Control, Chap 6, Peter Corke, Springer 2011

See also

Vehicle

RandomPath.RandomPath

Create a driver object

d = **RandomPath**(**dim**, **options**) returns a "driver" object capable of driving a Vehicle object through random waypoints. The waypoints are positioned inside a rectangular region bounded by +/- **dim** in the x- and y-directions.

Options

'speed', S	Speed along path (default 1m/s).
'dthresh', **d**	Distance from goal at which next goal is chosen.

See also

Vehicle

RandomPath.char

Convert to string

s = R.**char**() is a string showing driver parameters and state in in a compact human readable format.

RandomPath.demand

Compute speed and heading to waypoint

[**speed**,**steer**] = R.**demand**() returns the speed and steer angle to drive the vehicle toward the next waypoint. When the vehicle is within R.closeenough a new waypoint is chosen.

See also

Vehicle

RandomPath.display

Display driver parameters and state

R.**display**() displays driver parameters and state in compact human readable form.

See also

RandomPath.char

RandomPath.init

Reset random number generator

R.**init**() resets the random number generator used to create the waypoints. This enables the sequence of random waypoints to be repeated.

See also

randstream

RangeBearingSensor

Range and bearing sensor class

A concrete subclass of the Sensor class that implements a range and bearing angle sensor that provides robot-centric measurements of point features in the world. To enable this it has references to a map of the world (Map object) and a robot moving through the world (Vehicle object).

Methods

reading	range/bearing observation of random feature
h	range/bearing observation of specific feature
Hx	Jacobian matrix dh/dxv
Hxf	Jacobian matrix dh/dxf
Hw	Jacobian matrix dh/dw
g	feature positin given vehicle pose and observation
Gx	Jacobian matrix dg/dxv
Gz	Jacobian matrix dg/dz

Properties (read/write)

R	measurement covariance matrix (2×2)
interval	valid measurements returned every interval'th call to reading()

Reference

Robotics, Vision & Control, Chap 6, Peter Corke, Springer 2011

See also

Sensor, Vehicle, Map, EKF

RangeBearingSensor.RangeBearingSensor

Range and bearing sensor constructor

s = RangeBearingSensor(**vehicle**, **map**, **R**, **options**) is an object representing a range and bearing angle sensor mounted on the Vehicle object **vehicle** and observing an environment of known landmarks represented by the map object **map**. The sensor covariance is **R** (2×2) representing range and bearing covariance.

Options

'range', xmax	maximum range of sensor
'range', [xmin xmax]	minimum and maximum range of sensor
'angle', TH	detection for angles betwen -TH to +TH
'angle', [THMIN THMAX]	detection for angles betwen THMIN and THMAX
'skip', I	return a valid reading on every I'th call
'fail', [TMIN TMAX]	sensor simulates failure between timesteps TMIN and TMAX

See also

Sensor, Vehicle, Map, EKF

RangeBearingSensor.g

Compute landmark location

p = S.g(**xv**, **z**) is the world coordinate (1×2) of a feature given the sensor observation **z** (1×2) and vehicle state **xv** (3×1).

See also

RangeBearingSensor.Gx, RangeBearingSensor.Gz

RangeBearingSensor.Gx

Jacobian dg/dx

J = S.Gx(**xv**, **z**) is the Jacobian dg/dxv (2×3) at the vehicle state **xv** (3×1) for sensor observation **z** (2×1).

See also

RangeBearingSensor.g

RangeBearingSensor.Gz

Jacobian dg/dz

J = S.**Gz**(**xv**, **z**) is the Jacobian dg/dz (2×2) at the vehicle state **xv** (3×1) for sensor observation **z** (2×1).

See also

RangeBearingSensor.g

RangeBearingSensor.h

Landmark range and bearing

z = S.**h**(**xv**, **J**) is a sensor observation (1×2), range and bearing, from vehicle at pose **xv** (1×3) to the map feature K.

z = S.**h**(**xv**, **xf**) as above but compute range and bearing to a feature at coordinate **xf**.

Notes

- Supports vectorized operation where **xv** ($N \times 3$) and **z** ($N \times 2$).

See also

RangeBearingSensor.Hx, RangeBearingSensor.Hw, RangeBearingSensor.Hxf

RangeBearingSensor.Hw

Jacobian dh/dv

J = S.**Hw**(**xv**, **k**) is the Jacobian dh/dv (2×2) at the vehicle state **xv** (3×1) for map feature **k**.

See also

RangeBearingSensor.h

RangeBearingSensor.Hx

Jacobian dh/dxv

J = S.**Hx**(**xv**, **k**) returns the Jacobian dh/dxv (2×3) at the vehicle state **xv** (3×1) for map feature **k**.

J = S.**Hx**(**xv**, **xf**) as above but for a feature at coordinate **xf**.

See also

RangeBearingSensor.h

RangeBearingSensor.Hxf

Jacobian dh/dxf

J = S.**Hxf**(**xv**, **k**) is the Jacobian dh/dxv (2×2) at the vehicle state **xv** (3×1) for map feature **k**.

J = S.**Hxf**(**xv**, **xf**) as above but for a feature at coordinate **xf** (1×2).

See also

RangeBearingSensor.h

RangeBearingSensor.reading

Landmark range and bearing

[**z**,**k**] = S.**reading**() is an observation of a random landmark where **z**=[R,THETA] is the range and bearing with additive Gaussian noise of covariance R (specified to the constructor). **k** is the index of the map feature that was observed. If no valid measurement, ie. no features within range, interval subsampling enabled or simulated failure the return is **z**=[] and **k**=NaN.

See also

RangeBearingSensor.h

---

rotx

Rotation about X axis

R = **rotx**(**theta**) is a rotation matrix representing a rotation of **theta** radians about the x-axis.

R = **rotx**(**theta**, 'deg') as above but **theta** is in degrees.

See also

roty, rotz, angvec2r

---

roty

Rotation about Y axis

R = **roty**(**theta**) is a rotation matrix representing a rotation of **theta** radians about the y-axis.

R = **roty**(**theta**, 'deg') as above but **theta** is in degrees.

See also

rotx, rotz, angvec2r

---

rotz

Rotation about Z axis

R = rotz(**theta**) is a rotation matrix representing a rotation of **theta** radians about the z-axis.

R = rotz(**theta**, 'deg') as above but **theta** is in degrees.

See also

rotx, roty, angvec2r

---

rpy2jac

Jacobian from RPY angle rates to angular velocity

J = rpy2jac(**eul**) is a Jacobian matrix (3×3) that maps roll-pitch-yaw angle rates to angular velocity at the operating point RPY=[R,P,Y].

J = rpy2jac(**R**, **p**, **y**) as above but the roll-pitch-yaw angles are passed as separate arguments.

Notes

- Used in the creation of an analytical Jacobian.

See also

eul2jac, SerialLink.JACOBN

---

rpy2r

Roll-pitch-yaw angles to rotation matrix

R = rpy2r(**rpy**, **options**) is an orthonormal rotation matrix equivalent to the specified roll, pitch, yaw angles which correspond to rotations about the X, Y, Z axes respec-

tively. If **rpy** has multiple rows they are assumed to represent a trajectory and **R** is a three dimensional matrix, where the last index corresponds to the rows of **rpy**.

R = rpy2r(**roll**, **pitch**, **yaw**, **options**) as above but the roll-pitch-yaw angles are passed as separate arguments. If **roll**, **pitch** and **yaw** are column vectors they are assumed to represent a trajectory and **R** is a three dimensional matrix, where the last index corresponds to the rows of **roll**, **pitch**, **yaw**.

Options

'deg'	Compute angles in degrees (radians default)
'zyx'	Return solution for sequential rotations about Z, Y, X axes (Paul book)

Note

- In previous releases (<8) the angles corresponded to rotations about ZYX. Many texts (Paul, Spong) use the rotation order ZYX. This old behaviour can be enabled by passing the option 'zyx'

See also

tr2rpy, eul2tr

---

rpy2tr

Roll-pitch-yaw angles to homogeneous transform

T = rpy2tr(**rpy**, **options**) is a homogeneous transformation equivalent to the specified roll, pitch, yaw angles which correspond to rotations about the X, Y, Z axes respectively. If **rpy** has multiple rows they are assumed to represent a trajectory and **T** is a three dimensional matrix, where the last index corresponds to the rows of **rpy**.

T = rpy2tr(**roll**, **pitch**, **yaw**, **options**) as above but the roll-pitch-yaw angles are passed as separate arguments. If **roll**, **pitch** and **yaw** are column vectors they are assumed to represent a trajectory and **T** is a three dimensional matrix, where the last index corresponds to the rows of **roll**, **pitch**, **yaw**.

Options

'deg'	Compute angles in degrees (radians default)
'zyx'	Return solution for sequential rotations about Z, Y, X axes (Paul book)

Note

- In previous releases (<8) the angles corresponded to rotations about ZYX. Many texts (Paul, Spong) use the rotation order ZYX. This old behaviour can be enabled by passing the option 'zyx'

See also

tr2rpy, rpy2r, eul2tr

RRT

Class for rapidly-exploring random tree navigation

A concrete subclass of the Navigation class that implements the rapidly exploring random tree (RRT) algorithm. This is a kinodynamic planner that takes into account the motion constraints of the vehicle.

Methods

plan	Compute the tree
path	Compute a path
plot	Display the tree
display	Display the parameters in human readable form
char	Convert to string

Example

```
goal = [0,0];
start = [0,2,0];
veh = Vehicle([], 'stlim', 1.2);
rrt = RRT([], veh, 'goal', goal, 'range', 5);
rrt.plan()             % create navigation tree
rrt.path(start, goal)  % animate path from this start location
```

Robotics, Vision & Control compatability mode:

```
goal = [0,0];
start = [0,2,0];
rrt = RRT();           % create navigation object
rrt.plan()             % create navigation tree
rrt.path(start, goal)  % animate path from this start location
```


References

- Randomized kinodynamic planning, S. LaValle and J. Kuffner, International Journal of Robotics Research vol. 20, pp. 378-400, May 2001.
- Probabilistic roadmaps for path planning in high dimensional configuration spaces, L. Kavraki, P. Svestka, J. Latombe, and M. Overmars, IEEE Transactions on Robotics and Automation, vol. 12, pp. 566-580, Aug 1996.
- Robotics, Vision & Control, Section 5.2.5, P. Corke, Springer 2011.

See also

Navigation, PRM, DXform, Dstar, PGraph

RRT.RRT

Create a RRT navigation object

R = **RRT.RRT**(**map**, **veh**, **options**) is a rapidly exploring tree navigation object for a region with obstacles defined by the map object **map**.

R = **RRT.RRT**() as above but internally creates a Vehicle class object and does not support any **map** or **options**. For compatibility with RVC book.

Options

'npoints', N	Number of nodes in the tree
'time', T	Period to simulate dynamic model toward random point
'range', **R**	Specify rectangular bounds

- **R** scalar; X: -**R** to +**R**, Y: -**R** to +**R**
- **R** (1×2); X: -**R**(1) to +**R**(1), Y: -**R**(2) to +**R**(2)
- **R** (1×4); X: **R**(1) to **R**(2), Y: **R**(3) to **R**(4)

'goal', P	Goal position (1×2) or pose (1×3) in workspace
'speed', S	Speed of vehicle [m/s] (default 1)
'steermax', S	Maximum steer angle of vehicle [rad] (default 1.2)

Notes

- Does not (yet) support obstacles, ie. **map** is ignored but must be given.
- 'steermax' selects the range of steering angles that the vehicle will be asked to track. If not given the steering angle range of the vehicle will be used.

- There is no check that the steering range or speed is within the limits of the vehicle object.

Reference

- Robotics, Vision & Control Peter Corke, Springer 2011. p102.

See also

Vehicle

RRT.char

Convert to string

R.**char**() is a string representing the state of the **RRT** object in human-readable form.

invoke the superclass **char**() method

RRT.path

Find a path between two points

x = R.**path**(**start**, **goal**) finds a **path** ($N \times 3$) from state **start** (1×3) to the **goal** (1×3).

P.**path**(**start**, **goal**) as above but plots the **path** in 3D. The nodes are shown as circles and the line segments are blue for forward motion and red for backward motion.

Notes

- The **path** starts at the vertex closest to the **start** state, and ends at the vertex closest to the **goal** state. If the tree is sparse this might be a poor approximation to the desired start and end.

RRT.plan

Create a rapidly exploring tree

R.**plan**(**options**) creates the tree roadmap by driving the vehicle model toward random goal points. The resulting graph is kept within the object.

Options

'goal', P	Goal pose (1×3)
'noprogress'	Don't show the progress bar
'samples'	Show samples

- '.' for each random point x_rand
- 'o' for the nearest point which is added to the tree
- red line for the best path

RRT.plot

Visualize navigation environment

R.**plot**() displays the navigation tree in 3D.

---

rt2tr

Convert rotation and translation to homogeneous transform

TR = **rt2tr**(**R**, **t**) is a homogeneous transformation matrix ($M \times M$) formed from an orthonormal rotation matrix **R** ($N \times N$) and a translation vector **t** ($N \times 1$) where M=N+1.

For a sequence **R** ($N \times N \times K$) and **t** (kxN) results in a transform sequence (NxNxk).

Notes

- Works for **R** in SO(2) or SO(3)
  - If **R** is 2×2 and **t** is 2×1, then **TR** is 3×3
  - If **R** is 3×3 and **t** is 3×1, then **TR** is 4×4
- The validity of **R** is not checked

See also

t2r, r2t, tr2rt

---

rtdemo

Robot toolbox demonstrations

Displays popup menu of toolbox demonstration scripts that illustrate:

- homogeneous transformations
- trajectories
- forward kinematics
- inverse kinematics
- robot animation
- inverse dynamics
- forward dynamics

Notes

- The scripts require the user to periodically hit <Enter> in order to move through the explanation.
- Set PAUSE OFF if you want the scripts to run completely automatically.

---

se2

Create planar translation and rotation transformation

T = **se2**(**x**, **y**, **theta**) is a 3×3 homogeneous transformation SE(2) representing translation **x** and **y**, and rotation **theta** in the plane.

T = **se2**(**xy**) as above where **xy**=[**x**,**y**] and rotation is zero

T = **se2**(**xy**, **theta**) as above where **xy**=[**x**,**y**]

T = **se2**(**xyt**) as above where **xyt**=[**x**,**y**,**theta**]

See also

trplot2

Sensor

Sensor superclass

An abstact superclass to represent robot navigation sensors.

Methods

display	print the parameters in human readable form
char	convert to string

Properties

robot	The Vehicle object on which the sensor is mounted
map	The Map object representing the landmarks around the robot

Reference

Robotics, Vision & Control, Peter Corke, Springer 2011

See also

EKF, Vehicle, Map

Sensor.Sensor

Sensor object constructor

s = Sensor(**vehicle**, **map**) is a sensor mounted on the Vehicle object **vehicle** and observing the landmark map **map**. **s** = Sensor(**vehicle**, **map**, R) is an instance of the Sensor object mounted on a vehicle represented by the object **vehicle** and observing features in the world represented by the object **map**.

Sensor.char

Convert sensor parameters to a string

s = S.char() is a string showing sensor parameters in a compact human readable format.

Sensor.display

Display status of sensor object

S.**display**() displays the state of the sensor object in human-readable form.

Notes

- This method is invoked implicitly at the command line when the result of an expression is a Sensor object and the command has no trailing semicolon.

See also

Sensor.char

---

skew

Create skew-symmetric matrix

s = **skew**(**v**) is a **skew**-symmetric matrix formed from **v** (3×1).

```
| 0   -vz   vy|
| vz    0  -vx|
|-vy    vx   0 |
```

See also

vex

---

startup_rtb

Initialize MATLAB paths for Robotics Toolbox

Adds demos, examples to the MATLAB path, and adds also to Java class path.

---

t2r

Return rotational submatrix of a homogeneous transformation

R = t2r(**T**) is the orthonormal rotation matrix component of homogeneous transformation matrix **T**:

Notes

- Works for **T** in SE(2) or SE(3)
  - If **T** is 4×4, then **R** is 3×3.
  - If **T** is 3×3, then **R** is 2×2.
- The validity of rotational part is not checked
- For a homogeneous transform sequence returns a rotation matrix sequence

See also

r2t, tr2rt, rt2tr

---

tb_optparse

Standard option parser for Toolbox functions

[**optout**,**args**] = TB_OPTPARSE(**opt**, **arglist**) is a generalized option parser for Toolbox functions. It supports options that have an assigned value, boolean or enumeration types (string or int).

The software pattern is:

```
function(a, b, c, varargin)
opt.foo = true;
opt.bar = false;
opt.blah = [];
opt.choose = {'this', 'that', 'other'};
opt.select = {'#no', '#yes'};
opt = tb_optparse(opt, varargin);
```

Optional arguments to the function behave as follows:

'foo'	sets opt.foo <- true
'nobar'	sets opt.foo <- false
'blah', 3	sets opt.blah <- 3
'blah', x,y	sets opt.blah <- x,y
'that'	sets opt.choose <- 'that'
'yes'	sets opt.select <- 2 (the second element)

and can be given in any combination.

If neither of 'this', 'that' or 'other' are specified then opt.choose <- 'this'. Alternatively if:

```
opt.choose = {[], 'this', 'that', 'other'};
```

then if neither of 'this', 'that' or 'other' are specified then opt.choose <- []

If neither of 'no' or 'yes' are specified then opt.select <- 1.

Note:

- That the enumerator names must be distinct from the field names.
- That only one value can be assigned to a field, if multiple values

```
are required they must be converted to a cell array.
```

- To match an option that starts with a digit, prefix it with 'd_', so the field 'd_3d' matches the option '3d'.

The allowable options are specified by the names of the fields in the structure opt. By default if an option is given that is not a field of opt an error is declared.

Sometimes it is useful to collect the unassigned options and this can be achieved using a second output argument

```
[opt,arglist] = tb_optparse(opt, varargin);
```

which is a cell array of all unassigned arguments in the order given in varargin.

The return structure is automatically populated with fields: verbose and debug. The following options are automatically parsed:

'verbose'	sets opt.verbose <- true
'verbose=2'	sets opt.verbose <- 2 (very verbose)
'verbose=3'	sets opt.verbose <- 3 (extremeley verbose)
'verbose=4'	sets opt.verbose <- 4 (ridiculously verbose)
'debug', N	sets opt.debug <- N
'setopt', S	sets opt <- S
'showopt'	displays opt and arglist

tpoly

Generate scalar polynomial trajectory

[**s**,**sd**,**sdd**] = **tpoly**(**s0**, **sf**, **m**) is a scalar trajectory (**m** $\times$ 1) that varies smoothly from **s0** to **sf** in **m** steps using a quintic (5th order) polynomial. Velocity and acceleration can be optionally returned as **sd** (**m** $\times$ 1) and **sdd** (**m** $\times$ 1).

[**s**,**sd**,**sdd**] = **tpoly**(**s0**, **sf**, **T**) as above but specifies the trajectory in terms of the length of the time vector **T** (**m** $\times$ 1).

Notes

- If no output arguments are specified **s**, **sd**, and **sdd** are plotted.

---

tr2angvec

Convert rotation matrix to angle-vector form

[**theta**,**v**] = **tr2angvec**(**R**) converts an orthonormal rotation matrix **R** into a rotation of **theta** (1 $\times$ 1) about the axis **v** (1 $\times$ 3).

[**theta**,**v**] = **tr2angvec**(**T**) as above but uses the rotational part of the homogeneous transform **T**.

If **R** ($3 \times 3 \times K$) or **T** ($4 \times 4 \times K$) represent a sequence then **theta** ($K \times 1$)is a vector of angles for corresponding elements of the sequence and **v** ($K \times 3$) are the corresponding axes, one per row.

Notes

- If no output arguments are specified the result is displayed.
- This algorithm is from Paul 1981, other solutions are possible using eigenvectors or Rodriguez formula.

See also

angvec2r, angvec2tr

---

tr2delta

Convert homogeneous transform to differential motion

d = **tr2delta**(**T0**, **T1**) is the differential motion (6×1) corresponding to infinitessimal motion from pose **T0** to **T1** which are homogeneous transformations. **d**=(dx, dy, dz, dRx, dRy, dRz) and is an approximation to the average spatial velocity multiplied by time.

d = **tr2delta**(**T**) is the differential motion corresponding to the infinitessimal relative pose **T** expressed as a homogeneous transformation.

Notes

- **d** is only an approximation to the motion **T**, and assumes that **T0** **T1** or **T** eye(4,4).

See also

delta2tr, skew

---

tr2eul

Convert homogeneous transform to Euler angles

eul = **tr2eul**(**T**, **options**) are the ZYZ Euler angles expressed as a row vector corresponding to the rotational part of a homogeneous transform **T**. The 3 angles **eul**=[PHI,THETA,PSI] correspond to sequential rotations about the Z, Y and Z axes respectively.

eul = **tr2eul**(**R**, **options**) are the ZYZ Euler angles expressed as a row vector corresponding to the orthonormal rotation matrix **R**.

If **R** or **T** represents a trajectory (has 3 dimensions), then each row of **eul** corresponds to a step of the trajectory.

Options

'deg' Compute angles in degrees (radians default)

Notes

- There is a singularity for the case where THETA=0 in which case PHI is arbitrarily set to zero and PSI is the sum (PHI+PSI).

See also

eul2tr, tr2rpy

---

tr2jac

Jacobian for differential motion

J = **tr2jac**(**T**) is a Jacobian matrix (6×6) that maps spatial velocity or differential motion from the world frame to the frame represented by the homogeneous transform **T**.

See also

wtrans, tr2delta, delta2tr

---

tr2rpy

Convert a homogeneous transform to roll-pitch-yaw angles

rpy = **tr2rpy**(**T**, **options**) are the roll-pitch-yaw angles expressed as a row vector corresponding to the rotation part of a homogeneous transform **T**. The 3 angles **rpy**=[R,P,Y] correspond to sequential rotations about the X, Y and Z axes respectively.

rpy = **tr2rpy**(**R**, **options**) are the roll-pitch-yaw angles expressed as a row vector corresponding to the orthonormal rotation matrix **R**.

If **R** or **T** represents a trajectory (has 3 dimensions), then each row of **rpy** corresponds to a step of the trajectory.

Options

'deg'	Compute angles in degrees (radians default)
'zyx'	Return solution for sequential rotations about Z, Y, X axes (Paul book)

Notes

- There is a singularity for the case where P=pi/2 in which case **R** is arbitrarily set to zero and Y is the sum (**R**+Y).
- Note that textbooks (Paul, Spong) use the rotation order ZYX.

See also

rpy2tr, tr2eul

---

tr2rt

Convert homogeneous transform to rotation and translation

[**R**,**t**] = **tr2rt**(**TR**) split a homogeneous transformation matrix ($N \times N$) into an orthonormal rotation matrix **R** ($M \times M$) and a translation vector **t** ($M \times 1$), where N=M+1.

A homogeneous transform sequence **TR** ($N \times N \times K$) is split into rotation matrix sequence **R** ($M \times M \times K$) and a translation sequence **t** ($K \times M$).

Notes

- Works for **TR** in SE(2) or SE(3)
  - If **TR** is 4×4, then **R** is 3×3 and T is 3×1.
  - If **TR** is 3×3, then **R** is 2×2 and T is 2×1.
- The validity of **R** is not checked.

See also

rt2tr, r2t, t2r

---

tranimate

Animate a coordinate frame

tranimate(**p1**, **p2**, **options**) animates a 3D coordinate frame moving from pose **p1** to pose **p2**. Poses **p1** and **p2** can be represented by:

- homogeneous transformation matrices (4×4)
- orthonormal rotation matrices (3×3)
- Quaternion

tranimate(**p**, **options**) animates a coordinate frame moving from the identity pose to the pose **p** represented by any of the types listed above.

tranimate(**pseq**, **options**) animates a trajectory, where **pseq** is any of

- homogeneous transformation matrix sequence ($4 \times 4 \times N$)
- orthonormal rotation matrix sequence ($3 \times 3 \times N$)
- Quaternion vector ($N \times 1$)

Options

'fps', fps	Number of frames per second to display (default 10)
'nsteps', n	The number of steps along the path (default 50)
'axis', A	Axis bounds [xmin, xmax, ymin, ymax, zmin, zmax]

See also

trplot

---

transl

Create translational transform

T = **transl**(**x**, **y**, **z**) is a homogeneous transform representing a pure translation.

T = **transl**(**p**) is a homogeneous transform representing a translation or point **p**=[**x**,**y**,**z**]. If **p** ($M \times 3$) it represents a sequence and **T** ($4 \times 4 \times M$) is a sequence of homogenous transforms such that **T**(:,:,i) corresponds to the i'th row of **p**.

p = **transl**(**T**) is the translational part of a homogenous transform as a 3-element column vector. If **T** ($4 \times 4 \times M$) is a homgoeneous transform sequence the rows of **p**

($M \times 3$) are the translational component of the corresponding transform in the sequence.

Notes

- Somewhat unusually this function performs a function and its inverse. An historical anomaly.

See also

ctraj

---

trinterp

Interpolate homogeneous transformations

T = **trinterp**(**T0**, **T1**, **s**) is a homogeneous transform interpolation between **T0** when **s**=0 to **T1** when **s**=1. Rotation is interpolated using quaternion spherical linear interpolation. If **s** ($N \times 1$) then **T** ($4 \times 4 \times N$) is a sequence of homogeneous transforms corresponding to the interpolation values in **s**.

T = **trinterp**(**T**, **s**) is a transform that varies from the identity matrix when **s**=0 to **T** when R=1. If **s** ($N \times 1$) then **T** ($4 \times 4 \times N$) is a sequence of homogeneous transforms corresponding to the interpolation values in **s**.

See also

ctraj, quaternion

---

trnorm

Normalize a homogeneous transform

tn = **trnorm**(**T**) is a normalized homogeneous transformation matrix in which the rotation submatrix R = [N,O,A] is guaranteed to be a proper orthogonal matrix. The O and A vectors are normalized and the normal vector is formed from N = O x A, and then we ensure that O and A are orthogonal by O = A x N.

Notes

- Used to prevent finite word length arithmetic causing transforms to become 'unnormalized'.

See also

oa2tr

---

trotx

Rotation about X axis

T = **trotx**(**theta**) is a homogeneous transformation (4×4) representing a rotation radians about the x-axis.

T = **trotx**(**theta**, 'deg') as above but **theta** is in degrees.

Notes

- Translational component is zero.

See also

rotx, troty, trotz

---

troty

Rotation about Y axis

T = **troty**(**theta**) is a homogeneous transformation (4×4) representing a rotation radians about the y-axis.

T = **troty**(**theta**, 'deg') as above but **theta** is in degrees.

Notes

- Translational component is zero.

See also

roty, trotx, trotz

---

trotz

Rotation about Z axis

T = **trotz**(**theta**) is a homogeneous transformation (4×4) representing a rotation radians about the z-axis.

T = **trotz**(**theta**, 'deg') as above but **theta** is in degrees.

Notes

- Translational component is zero.

See also

rotz, trotx, troty

---

trplot

Draw a coordinate frame

trplot(**T**, **options**) draws a 3D coordinate frame represented by the homogeneous transform **T** (4×4).

H = **trplot**(**T**, **options**) as above but returns a handle.

trplot(**H**, **T**) moves the coordinate frame described by the handle **H** to the pose **T** (4×4).

trplot(**R**, **options**) draws a 3D coordinate frame represented by the orthonormal rotation matrix **R** (3×3).

H = **trplot**(**R**, **options**) as above but returns a handle.

trplot(**H**, **R**) moves the coordinate frame described by the handle **H** to the orientation **R**.

Options

'color', C	The color to draw the axes, MATLAB colorspec C
'noaxes'	Don't display axes on the plot
'axis', A	Set dimensions of the MATLAB axes to A=[xmin xmax ymin ymax zmin zmax]
'frame', F	The frame is named F and the subscript on the axis labels is F.
'text_opts', opt	A cell array of MATLAB text properties
'handle', **H**	Draw in the MATLAB axes specified by the axis handle **H**
'view', V	Set plot view parameters V=[az el] angles, or 'auto' for view toward origin of coordinate frame
'arrow'	Use arrows rather than line segments for the axes
'width', w	Width of arrow tips
'3d'	Plot in 3D using anaglyph graphics
'anaglyph', A	Specify anaglyph colors for '3d' as 2 characters for left and right (default colors 'rc'):

```
'r'   red
'g'   green
'b'   green
'c'   cyan
'm'   magenta
```

'dispar', D Disparity for 3d display (default 0.1)

Examples

```
trplot(T, 'frame', 'A')
trplot(T, 'frame', 'A', 'color', 'b')
trplot(T1, 'frame', 'A', 'text_opts', {'FontSize', 10, 'FontWeight', 'bold'})
```

```
h = trplot(T, 'frame', 'A', 'color', 'b');
trplot(h, T2);
```

3D anaglyph plot

```
trplot(T, '3d');
```

Notes

- The arrow option requires the third party package arrow3.
- The handle **H** is an hgtransform object.
- When using the form **trplot**(**H**, ...) the axes are not rescaled.
- The '3d' option requires that the plot is viewed with anaglyph glasses.
- You cannot specify 'color'

See also

trplot2, tranimate

trplot2

Plot a planar transformation

trplot2(**T**, **options**) draws a 2D coordinate frame represented by the SE(2) homogeneous transform **T** (3×3).

H = **trplot2**(**T**, **options**) as above but returns a handle.

trplot2(**H**, **T**) moves the coordinate frame described by the handle **H** to the SE(2) pose **T** (3×3).

Options

'axis', A	Set dimensions of the MATLAB axes to A=[xmin xmax ymin ymax]
'color', c	The color to draw the axes, MATLAB colorspec
'noaxes'	Don't display axes on the plot
'frame', F	The frame is named F and the subscript on the axis labels is F.
'text_opts', opt	A cell array of Matlab text properties
'handle', h	Draw in the MATLAB axes specified by h
'view', V	Set plot view parameters V=[az el] angles, or 'auto' for view toward origin of coordinate frame
'arrow'	Use arrows rather than line segments for the axes
'width', w	Width of arrow tips

Examples

```
trplot(T, 'frame', 'A')
trplot(T, 'frame', 'A', 'color', 'b')
trplot(T1, 'frame', 'A', 'text_opts', {'FontSize', 10, 'FontWeight', 'bold'})
```

Notes

- The arrow option requires the third party package arrow3.
- Generally it is best to set the axis bounds

See also

trplot

trprint

Compact display of homogeneous transformation

trprint(**T**, **options**) displays the homogoneous transform in a compact single-line format. If **T** is a homogeneous transform sequence then each element is printed on a separate line.

s = **trprint**(**T**, **options**) as above but returns the string.

trprint T is the command line form of above, and displays in RPY format.

Options

'rpy'	display with rotation in roll/pitch/yaw angles (default)
'euler'	display with rotation in ZYX Euler angles
'angvec'	display with rotation in angle/vector format
'radian'	display angle in radians (default is degrees)
'fmt', f	use format string f for all numbers, (default %g)
'label', l	display the text before the transform

Examples

```
>> trprint(T2)
t = (0,0,0), RPY = (-122.704,65.4084,-8.11266) deg

>> trprint(T1, 'label', 'A')

A:t = (0,0,0), RPY = (-0,0,-0) deg
```

See also

tr2eul, tr2rpy, tr2angvec

---

unit

Unitize a vector

vn = **unit**(**v**) is a **unit** vector parallel to **v**.

Note

- Reports error for the case where norm(**v**) is zero.

Vehicle

Car-like vehicle class

This class models the kinematics of a car-like vehicle (bicycle model). For given steering and velocity inputs it updates the true vehicle state and returns noise-corrupted odometry readings.

Methods

init	initialize vehicle state
f	predict next state based on odometry
step	move one time step and return noisy odometry
control	generate the control inputs for the vehicle
update	update the vehicle state
run	run for multiple time steps
Fx	Jacobian of f wrt x
Fv	Jacobian of f wrt odometry noise
gstep	like step() but displays vehicle
plot	plot/animate vehicle on current figure
plot_xy	plot the true path of the vehicle
add_driver	attach a driver object to this vehicle
display	display state/parameters in human readable form
char	convert to string

Static methods

plotv	plot/animate a pose on current figure

Properties (read/write)

x	true vehicle state (3×1)
V	odometry covariance (2×2)
odometry	distance moved in the last interval (2×1)
rdim	dimension of the robot (for drawing)
L	length of the vehicle (wheelbase)
alphalim	steering wheel limit
maxspeed	maximum vehicle speed
T	sample interval
verbose	verbosity
x_hist	history of true vehicle state ($N \times 3$)
driver	reference to the driver object
x0	initial state, restored on init()

Examples

Create a vehicle with odometry covariance

```
v = Vehicle( diag([0.1 0.01].^2 );
```

and display its initial state

```
v
```

now apply a speed (0.2m/s) and steer angle (0.1rad) for 1 time step

```
odo = v.update([0.2, 0.1])
```

where odo is the noisy odometry estimate, and the new true vehicle state

```
v
```

We can add a driver object

```
v.add_driver( RandomPath(10) )
```

which will move the vehicle within the region -10<x<10, -10<y<10 which we can see by

```
v.run(1000)
```

which shows an animation of the vehicle moving between randomly selected wayoints.

Notes

- Subclasses the MATLAB handle class which means that pass by reference semantics apply.

Reference

Robotics, Vision & Control, Peter Corke, Springer 2011

See also

RandomPath, EKF

Vehicle.Vehicle

Vehicle object constructor

v = Vehicle(**v**_ACT, **options**) creates a Vehicle object with actual odometry covariance **v**_ACT (2×2) matrix corresponding to the odometry vector [dx dtheta].

Options

'stlim', A	Steering angle limit (default 0.5 rad)
'vmax', S	Maximum speed (default 5m/s)
'L', L	Wheel base (default 1m)
'x0', x0	Initial state (default (0,0,0))
'dt', T	Time interval
'rdim', R	Robot size as fraction of plot window (default 0.2)
'verbose'	Be verbose

Notes

- Subclasses the MATLAB handle class which means that pass by reference semantics apply.

Vehicle.add_driver

Add a driver for the vehicle

V.add_driver(**d**) connects a driver object **d** to the vehicle. The driver object has one public method:

```
[speed, steer] = D.demand();
```

that returns a speed and steer angle.

Notes

- The Vehicle.step() method invokes the driver if one is attached.

See also

Vehicle.step, RandomPath

Vehicle.char

Convert to a string

s = V.**char**() is a string showing vehicle parameters and state in in a compact human readable format.

See also

Vehicle.display

Vehicle.control

Compute the control input to vehicle

u = V.**control**(**speed**, **steer**) returns a **control** input (speed,steer) based on provided controls **speed**,**steer** to which speed and steering angle limits have been applied.

u = V.**control**() returns a **control** input (speed,steer) from a "driver" if one is attached, the driver's DEMAND() method is invoked. If no driver is attached then speed and steer angle are assumed to be zero.

See also

Vehicle.step, RandomPath

Vehicle.display

Display vehicle parameters and state

V.**display**() displays vehicle parameters and state in compact human readable form.

Notes

- This method is invoked implicitly at the command line when the result of an expression is a Vehicle object and the command has no trailing semicolon.

See also

Vehicle.char

Vehicle.f

Predict next state based on odometry

xn = V.f(**x**, **odo**) predict next state **xn** (1×3) based on current state **x** (1×3) and odometry **odo** (1×2) is [distance,change_heading].

xn = V.f(**x**, **odo**, **w**) as above but with odometry noise **w**.

Notes

- Supports vectorized operation where **x** and **xn** $(N \times 3)$.

Vehicle.Fv

Jacobian df/dv

J = V.Fv(**x**, **odo**) returns the Jacobian df/dv (3×2) at the state **x**, for odometry input **odo**.

See also

Vehicle.F, Vehicle.Fx

Vehicle.Fx

Jacobian df/dx

J = V.Fx(**x**, **odo**) is the Jacobian df/dx (3×3) at the state **x**, for odometry input **odo**.

See also

Vehicle.f, Vehicle.Fv

Vehicle.init

Reset state of vehicle object

V.**init**() sets the state V.x := V.x0, initializes the driver object (if attached) and clears the history.

V.**init**(**x0**) as above but the state is initialized to **x0**.

Vehicle.plot

Plot vehicle

V.**plot**(**options**) plots the vehicle on the current axes at a pose given by the current state. If the vehicle has been previously plotted its pose is updated. The vehicle is depicted as a narrow triangle that travels "point first" and has a length V.rdim.

V.**plot**(**x**, **options**) plots the vehicle on the current axes at the pose **x**.

Vehicle.plot_xy

Plots true path followed by vehicle

V.plot_xy() plots the true xy-plane path followed by the vehicle.

V.plot_xy(**ls**) as above but the line style arguments **ls** are passed to plot.

Notes

- The path is extracted from the x_hist property.

Vehicle.plotv

Plot ground vehicle pose

H = **Vehicle.plotv**(**x**, **options**) draws a representation of a ground robot as an oriented triangle with pose **x** (1×3) [x,y,theta]. **H** is a graphics handle. If **x** $(N \times 3)$ is a matrix it is considered to represent a trajectory in which case the vehicle graphic is animated.

Vehicle.plotv(**H**, **x**) as above but updates the pose of the graphic represented by the handle **H** to pose **x**.

Options

'scale', S	Draw vehicle with length S x maximum axis dimension
'size', S	Draw vehicle with length S
'color', C	Color of vehicle.
'fill'	Filled with solid color as per 'color' option
'fps', F	Frames per second in animation mode (default 10)

Example

Generate some path $3 \times N$

```
p = PRM.plan(start, goal);
```

Set the axis dimensions to stop them rescaling for every point on the path

```
axis([-5 5 -5 5]);
```

Now invoke the static method

```
Vehicle.plotv(p);
```

Notes

- This is a static method.

Vehicle.run

Run the vehicle simulation

V.**run**(**n**) runs the vehicle model for **n** timesteps and plots the vehicle pose at each step.

p = V.**run**(**n**) runs the vehicle simulation for **n** timesteps and return the state history (**n** $\times$ 3) without plotting. Each row is (x,y,theta).

See also

Vehicle.step

Vehicle.run2

run the vehicle simulation

p = V.**run2**(**T**, **x0**, **speed**, **steer**) runs the vehicle model for a time **T** with speed **speed** and steering angle **steer**. **p** ($N \times 3$) is the path followed and each row is (x,y,theta).

Notes

- Faster and more specific version of run() method.

See also

Vehicle.run, Vehicle.step

Vehicle.step

Advance one timestep

odo = V.**step**(**speed**, **steer**) updates the vehicle state for one timestep of motion at specified **speed** and **steer** angle, and returns noisy odometry.

odo = V.**step**() updates the vehicle state for one timestep of motion and returns noisy odometry. If a "driver" is attached then its DEMAND() method is invoked to compute speed and steer angle. If no driver is attached then speed and steer angle are assumed to be zero.

Notes

- Noise covariance is the property V.

See also

Vehicle.control, Vehicle.update, Vehicle.add_driver

Vehicle.update

Update the vehicle state

odo = V.**update**(**u**) is the true odometry value for motion with **u**=[speed,steer].

Notes

- Appends new state to state history property x_hist.
- Odometry is also saved as property odometry.

Vehicle.verbosity

Set verbosity

V.**verbosity**(**a**) set **verbosity** to **a**. **a**=0 means silent.

---

vex

Convert skew-symmetric matrix to vector

v = **vex**(**s**) is the vector (3×1) which has the skew-symmetric matrix **s** (3×3)

```
| 0   -vz   vy|
| vz   0   -vx|
|-vy   vx   0 |
```

Notes

- This is the inverse of the function SKEW().
- No checking is done to ensure that the matrix is actually skew-symmetric.
- The function takes the mean of the two elements that correspond to each unique element of the matrix, ie. vx = 0.5*(**s**(3,2)-**s**(2,3))

See also

skew

---

wtrans

Transform a wrench between coordinate frames

wt = **wtrans**(**T**, **w**) is a wrench (6×1) in the frame represented by the homogeneous transform **T** (4×4) corresponding to the world frame wrench **w** (6×1).

The wrenches **w** and **wt** are 6-vectors of the form [Fx Fy Fz Mx My Mz].

See also

tr2delta, tr2jac

---

xaxis

Set X-axis scaling

xaxis(**max**) set x-axis scaling from 0 to **max**.

xaxis(**min**, **max**) set x-axis scaling from **min** to **max**.

xaxis([**min max**]) as above.

xaxis restore automatic scaling for x-axis.

---

xyzlabel

Label X, Y and Z axes

XYZLABEL label the x-, y- and z-axes with 'X', 'Y', and 'Z' respectiveley

---

yaxis

Y-axis scaling

yayis(**max**) **yayis**(min, **max**)

YAXIS restore automatic scaling for this axis
